

# Thermal Inflation with a Waterfall Field Mass Coupled to a Light Auxiliary Scalar Field

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# Outline

## 1 Thermal Inflation

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- 3 “End of Inflation” Mechanism
  - Generating  $\zeta$
  - Constraining the Free Parameters
  - Results

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- 4 Modulated Decay Rate

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- 5 Summary

# Thermal Inflation

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When temperature and mass terms of waterfall field are equal
- Solves the moduli problem

# Our New Model

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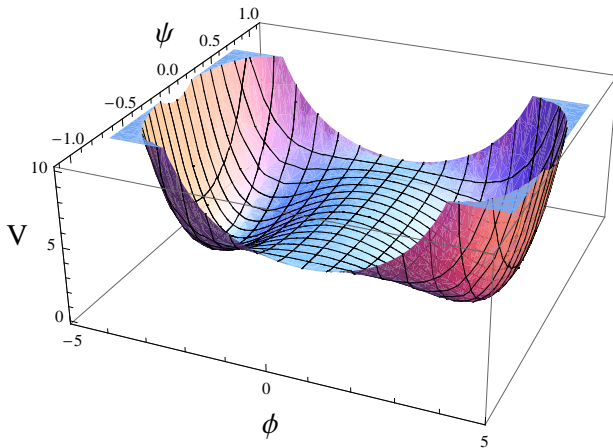
$\psi$ : Light auxiliary scalar field

$$V(\phi, T, \psi) = V_0 + (g^2 T^2 - \frac{1}{2} m^2) \phi^2 + \lambda_n \frac{\phi^{2n+4}}{M_{Pl}^{2n}} + \frac{1}{2} m_\psi^2 \psi^2$$

where

$$m^2 \equiv m_0^2 - 2h_\alpha^2 \frac{\psi^{2\alpha}}{M_{Pl}^{2\alpha-2}}$$

$$\alpha, n \geq 1$$



Arbitrary Units

We don't get domain walls, as we can interpret  $\phi$  as being the real part of a complex field, whose potential contains only 1 continuous VEV.

$T_1$  and  $T_2$ 

From

$$\rho_r = \frac{\pi^2}{30} g_* T^4$$

we obtain

$$T_1 \sim V_0^{\frac{1}{4}}$$

$$T_2 = \frac{m}{\sqrt{2}g}$$



## Other Quantities

$$\langle \phi \rangle = \left( \frac{m M_{Pl}^n}{\sqrt{(2n+4)\lambda_n}} \right)^{\frac{1}{n+1}}$$

$$V_0 \sim \left( \frac{m_0^{2n+4} M_{Pl}^{2n}}{\lambda_n} \right)^{\frac{1}{n+1}} \quad (V = 0 \text{ at the VEV})$$

$$H_{TI} \sim \left( \frac{m_0^{n+2}}{\sqrt{\lambda_n} M_{Pl}} \right)^{\frac{1}{n+1}}$$

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e-foldings

$$N = \ln \frac{a_2}{a_1} = \ln \frac{T_1}{T_2}$$

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Therefore we obtain

$$N \approx \ln \left( \frac{\sqrt{2} g V_0^{\frac{1}{4}}}{m} \right)$$

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$$N \approx \ln \left( \frac{\sqrt{2} g V_0^{\frac{1}{4}}}{m} \right)$$

$\delta N$  Formalism

$$\zeta = \delta N = \frac{dN}{dm} \delta m + \frac{1}{2!} \frac{d^2 N}{dm^2} \delta m^2 + \frac{1}{3!} \frac{d^3 N}{dm^3} \delta m^3 + \dots$$

Therefore we obtain, to 3<sup>rd</sup> order

$$\zeta = \delta N = -\frac{\delta m}{m} + \frac{1}{2} \frac{\delta m^2}{m^2} - \frac{1}{3} \frac{\delta m^3}{m^3}$$

Therefore we obtain, to 3<sup>rd</sup> order

$$\zeta = \delta N = -\frac{\delta m}{m} + \frac{1}{2} \frac{\delta m^2}{m^2} - \frac{1}{3} \frac{\delta m^3}{m^3}$$

Substituting  $m$  and  $\delta m$  into this gives us

$$\zeta = \delta N = \frac{1}{\pi} \frac{\alpha h_\alpha^2 H_* \psi^{2\alpha-1}}{m^2 M_{Pl}^{2\alpha-2}} + \frac{1}{2\pi^2} \left( \frac{\alpha h_\alpha^2 H_* \psi^{2\alpha-1}}{m^2 M_{Pl}^{2\alpha-2}} \right)^2 + \frac{1}{3\pi^3} \left( \frac{\alpha h_\alpha^2 H_* \psi^{2\alpha-1}}{m^2 M_{Pl}^{2\alpha-2}} \right)^3$$

where we have used

$$\delta\psi = \frac{H_*}{2\pi}$$

as the most probable value of  $\delta\psi$ .

# Constraining the Free Parameters

## Primordial Inflation Scale



# Constraining the Free Parameters

## Primordial Inflation Scale

We want the scale of primordial inflation to be

$$V^{\frac{1}{4}} \lesssim 10^{14} \text{ GeV}$$

Therefore, from

$$3M_{Pl}^2 H_*^2 = V$$

we require

$$H_* \lesssim 10^{10} \text{ GeV}$$

# Constraining the Free Parameters

## Inflationary Dynamics

# Constraining the Free Parameters

## Inflationary Dynamics

In order that the  $\psi$  field does not affect the inflationary dynamics during thermal inflation, we require, from our definition of  $m$ ,

$$m_0^2 \gg h_\alpha^2 \frac{\psi_*^{2\alpha}}{M_{Pl}^{2\alpha-2}}$$

Therefore we have

$$m \approx m_0$$

# Constraining the Free Parameters

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Make the field equation for  $\psi$  look like that of a free field, i.e. make the coupling term to  $\phi$  in the field equation sub-dominant.

From the field equation

$$\ddot{\psi} + 3H\dot{\psi} + \frac{\partial V}{\partial \psi} = 0$$

we obtain

$$\ddot{\psi} + 3H\dot{\psi} + m_{\psi}^2 \psi + 2\alpha h_{\alpha}^2 \frac{\psi^{2\alpha-1}}{M_{Pl}^{2\alpha-2}} \phi^2 = 0$$

Therefore, in order that the field equation looks like that of a free field, we require

$$m_\psi \gg h_\alpha \left( \frac{\psi_*}{M_{Pl}} \right)^{\alpha-1} \phi$$



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- Substituting the observed spectrum value

$$\mathcal{P}_\zeta^{\frac{1}{2}} = 4.9 \times 10^{-5}$$

into our equation for  $\zeta$  gives us the constraint

$$\psi_* \sim \left( \frac{10^{-4} m_0^2 M_{Pl}^{2\alpha-2}}{h_\alpha^2 H_*} \right)^{\frac{1}{2\alpha-1}}$$

- We require  $\psi_* \gg \delta\psi_*$ . Therefore we obtain, with  $\delta\psi_* \sim H_*$ ,

$$\psi_* \gg H_*$$

and

$$\frac{\delta\psi_*}{\psi_*} \ll 1$$

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$$m_{\psi,eff} \ll H_*$$

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We have

$$m_{\psi,eff}^2 = m_{\psi}^2 + (4\alpha^2 - 2\alpha)h_{\alpha}^2\phi^2 \left( \frac{\psi}{M_{Pl}} \right)^{2\alpha-2}$$

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Therefore, we require

$$m_{\psi} \ll H_*$$

and

$$h_{\alpha}\phi_* \left( \frac{\psi_*}{M_{Pl}} \right)^{\alpha-1} \ll H_*$$

Require  $\delta\psi$  to be frozen at their initial value coming from primordial inflation. If perturbations unfroze, would oscillate and therefore their amplitude would decay as  $a^{-\frac{3}{2}}$ , drastically reducing their effect on  $\psi$  later on during thermal inflation.

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This gives us the constraint

$$m_\psi \ll H_{TI}$$

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$\phi$  is in thermal equilibrium with the thermal bath.

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In order to keep  $m_{\psi,eff}$  light, we therefore require

$$h_{\alpha} T \left( \frac{\psi_*}{M_{Pl}} \right)^{\alpha-1} \ll H_{TI}$$

Assuming that thermal equilibrium occurs only at the onset of thermal inflation, i.e. when  $T \sim V_0^{\frac{1}{4}}$  and by substituting our expressions for  $H_{TI}$  and  $\psi_*$  into the above we obtain the constraint

$$h_\alpha \ll \frac{(10^4 H_*)^{\alpha-1}}{(\sqrt{\lambda_n})^{2\alpha-1} m_0^{2\alpha n-3n-2} M_{Pl}^{2\alpha+n})^{\frac{1}{2n+2}}}$$

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Rearranging this for  $m_0$  gives us the constraint

$$m_0 \ll \left( \frac{(10^4 H_*)^{(2\alpha-2)(n+1)}}{h_\alpha^{2n+2} \sqrt{\lambda_n}^{2\alpha-1} M_{Pl}^{2\alpha+n}} \right)^{\frac{1}{2\alpha n-3n-2}}$$

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Our potential will receive a SUGRA correction during primordial inflation of

$$\Delta V \sim c H_*^2 \phi_*^2$$

where  $c \sim 1$ .



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where  $c \sim 1$ .

We have

$$\phi_* \propto \sqrt{\rho} \propto a^{-\frac{3}{2}}$$

As  $a$  grows exponentially during inflation,  $\phi_*$  is driven rapidly to 0.

In order for the affect of the SUGRA correction on the potential to be present, we require  $\phi$  to be light during primordial inflation, giving us

$$m_{\phi, \text{eff}} \ll H_*$$

During primordial inflation the effective mass of  $\phi$  is

$$m_{\phi, \text{ prim. inf.}}^2 = -m_0^2 + 2h_\alpha^2 \frac{\psi_*^{2\alpha}}{M_{Pl}^{2\alpha-2}}$$
$$\sim -m_0^2$$

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$$\sim -m_0^2$$

Therefore we have the constraint

$$m_0 \ll H_*$$

Reason why we consider SUGRA correction is that if we ignored it, the constraints that we would obtain from keeping effective mass of  $\psi$  light when considering  $\phi_*$  are much tighter.

# Constraining the Free Parameters

Time for Transition from Thermal Inflation to Field Oscillation

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<sup>1</sup>D.H. Lyth, *JCAP* **1205** (2012) 022

# Constraining the Free Parameters

## Time for Transition from Thermal Inflation to Field Oscillation

In order for "end of inflation" mechanism to produce observed  $\zeta$ , the transition from thermal inflation to field oscillation has to be sufficiently fast<sup>1</sup>.

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We require

$$H_{TI} \ll 10^{-5} m_0$$

From this and by requiring  $H_{TI} \lesssim H_*$  and  $\psi_* \gg H_*$  we obtain

$$\psi_* \gg 10^{-6} m_0$$

and

$$\frac{\delta\psi_*}{\psi_*} \ll 10^6 \frac{H_*}{m_0}$$

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As  $\psi$  has acquired perturbations, we require it to not dominant energy density of universe after end of thermal inflation, at which time  $m_{\psi,eff}$  is increased significantly, becoming larger than  $H$ .

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Energy density of oscillating  $\psi$  field after end of thermal inflation is

$$\rho_{\psi,osc} \sim m_{\psi,osc}^2 \psi_*^2$$

Therefore we require

$$m_{\psi,osc}^2 \psi_*^2 \ll M_{Pl}^2 H_{TI}^2$$

This condition also guarantees that  $\psi$  energy density is subdominant all the way until  $\psi$  decays, as  $H$  will not have changed much from  $H_{TI}$  at the time of  $\psi$  decay, due to the rapid oscillations and subsequent decay of  $\psi$  which will not take very long.

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We have

$$m_{\psi,osc}^2 = m_{\psi}^2 + (4\alpha^2 - 2\alpha)h_{\alpha}^2\overline{\phi}^2 \left(\frac{\psi_*}{M_{Pl}}\right)^{2\alpha-2}$$
$$\sim h_{\alpha}^2\langle\phi\rangle^2 \left(\frac{\psi_*}{M_{Pl}}\right)^{2\alpha-2}$$

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$$\sim h_{\alpha}^2\langle\phi\rangle^2 \left( \frac{\psi_*}{M_{Pl}} \right)^{2\alpha-2}$$

Substituting this and our expressions for  $\langle\phi\rangle$  and  $H_{TI}$  into the previous equation gives us

$$h_{\alpha} \ll \frac{m_0 M_{Pl}^{\alpha-1}}{\psi_*^{\alpha}}$$

Substituting our expressions for  $\langle\phi\rangle$ ,  $H_{TI}$  and  $m_{\psi,osc}^2$  into

$$\frac{H_{TI}}{m_{\psi,osc}} < 1$$

gives us

$$h_\alpha > \frac{m_0 M_{Pl}^{\alpha-2}}{\psi_*^{\alpha-1}}$$



# Constraining the Free Parameters

## Other Constraints

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## Other Constraints

- We require

$$m \gtrsim 1 \text{ TeV}$$

If  $\phi$  were to have couplings only of gravitational strength, then we would require  $m \gtrsim 10 \text{ TeV}$ , so as to not affect BBN. However, as  $\phi$  interacts with the thermal bath,  $\psi$  and Standard Model fields and given that we have not observed  $\phi$  particles, the constraint on  $m$  is loosened down to 1 TeV.

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- To protect BBN we require

$$H_{TI} \gtrsim 10^{-3} \text{ GeV}$$

# Constraining the Free Parameters

## Combining Constraints

These are all of the constraints that come from the physics.

However, we obtain many more by substituting them into each other.

I will not show you these ones.

# Results

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When all of the constraints on  $m_0$  are applied, only a value of  $m_0 \sim 10^3$  GeV is allowed, subject to the following values:

$$H_* \sim 10^{10} \text{ GeV}$$

$$\alpha = 2$$

$$n = 1$$

$$\lambda_1 \sim 10^{-4} - 10^{-3}$$

$$\lambda_1 \sim 10^{-2} - 1$$

$$h_2 \sim 10^{-6} - 10^{-5}$$

$$h_2 \sim 10^{-7} - 10^{-4}$$

$$g \sim 10^{-5} - 1$$

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However, with these values, the constraints

$$m_\psi \gg \left( \frac{10^{-39} \text{ GeV}^{13}}{M_{Pl}} \right)^{\frac{1}{12}} \frac{h_2^{\frac{1}{3}}}{\lambda_1^{\frac{1}{8}}}$$

and

$$m_\psi \ll H_{TI}$$

cannot both be satisfied.

However, with these values, the constraints

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cannot both be satisfied.

**Therefore, there is no parameter space available for the "end of inflation" scenario.**



# Modulated Decay Rate

## Modulated Decay Rate

Now we investigate the modulated decay scenario to see if it can produce the dominant contribution to the primordial curvature perturbation.

The decay rate of  $\phi$  is

$$\Gamma \sim \frac{m_{\phi,osc}^3}{M_{Pl}^2}$$

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Therefore we obtain

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Differentiating this w.r.t.  $m$  gives us

$$\delta\Gamma \sim (2n + 3)^{\frac{3}{2}} \frac{m^2}{M_{Pl}^2} \delta m$$

The  $\zeta$  that is produced by a varying decay rate<sup>2</sup> going from field oscillation after thermal inflation to  $\phi$  decay is given to 1<sup>st</sup> order by

$$\zeta_{osc \rightarrow dec} = \delta N_{osc \rightarrow dec} = -\frac{1}{6} \frac{\delta \Gamma}{\Gamma}$$

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<sup>2</sup>G. Dvali, A. Gruzinov and M. Zaldarriaga, *Phys.Rev.* **D69** (2004) 023505

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$$\zeta_{osc \rightarrow dec} = \delta N_{osc \rightarrow dec} = -\frac{1}{6} \frac{\delta \Gamma}{\Gamma}$$

Substituting our expressions for  $\Gamma$  and  $\delta \Gamma$  into this gives us

$$\zeta_{osc \rightarrow dec} = \delta N_{osc \rightarrow dec} \sim -\frac{\delta m}{m}$$

This is of the same order as the  $\zeta$  produced by the “end of inflation” mechanism.

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<sup>2</sup>G. Dvali, A. Gruzinov and M. Zaldarriaga, *Phys.Rev.* **D69** (2004) 023505

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Substituting our expressions for  $\psi_*$  and  $\langle\phi\rangle$  into the constraint gives us

$$m_\psi \gg \left( \frac{10^{-4}}{H_*} \right)^{\frac{\alpha-1}{2\alpha-1}} \left( \frac{h^{n+1} m_0^{2\alpha n+4\alpha-2n-3} M_{Pl}^{\alpha n-\alpha+1}}{\sqrt{(2n+4)\lambda_n}^{2\alpha-1}} \right)^{\frac{1}{(2\alpha-1)(n+1)}}$$



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**When this and all other relevant constraints from “end of inflation” scenario are applied to modulated decay rate scenario, there is no parameter space available.**

# Summary

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- General thermal inflation model with a waterfall field mass coupled to a light auxiliary scalar field

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- **No parameter space available for the model and thus it is ruled out**
- *Paper to appear soon*

# Thank you

## Any questions?

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