

1 **Gas slug ascent in a stratified magma: implications of flow organisation**
2 **and instability for Strombolian eruption dynamics**

3 **A. Capponi, M.R. James, S.J. Lane**

4 *Lancaster Environment Centre, Lancaster University, Lancaster, LA1 4YQ, UK*

5 Corresponding author: Antonio Capponi, Lancaster Environment Centre, Lancaster
6 University, LA1 4YQ, UK, a.capponi@lancaster.ac.uk

7

8 **Abstract**

9 The canonical Strombolian paradigm of a gas slug ascending and bursting in a
10 homogenous low-viscosity magma cannot explain the complex details in eruptive dynamics
11 recently revealed by field measurements and textural and geochemical analyses. Evidence
12 points to the existence of high-viscosity magma at the top of the conduit of Strombolian-type
13 volcanoes, acting as a plug. Here, new experiments detail the range of flow configurations
14 that develop during the ascent and burst of a slug through rheologically stratified magma
15 within a conduit. End-member scenarios of a tube fully filled with either high- or low-
16 viscosity liquid bracket three main flow configurations: (1) a plug sufficiently large to fully
17 accommodate an ascending gas slug. (2) A plug that can accommodate the intrusion of low-
18 viscosity liquid driven by the gas expansion, but not all the slug volume, so the slug bursts
19 with the nose in the plug whilst the base is still in the low-viscosity liquid. (3) Gas expansion
20 is sufficient to drive the intrusion of low-viscosity liquid through the plug, with the slug
21 bursting in the low-viscosity layer emplaced dynamically above the plug. We show that the
22 same flow configurations are viable at volcanic-scale through a new experimentally-validated
23 1D model and 3D computational fluid dynamic simulations. Applied to Stromboli, our results
24 demonstrate that the key parameters controlling the transition between each configuration are
25 gas volume, plug thickness and plug viscosity. The flow processes identified include effective
26 dynamic narrowing and widening of the conduit, instabilities within the falling magma film,
27 transient partial and complete blockage of the conduit, and slug disruption. These
28 complexities influence eruption dynamics and vigour, promoting magma mingling and
29 resulting in pulsatory release of gas.

30 **Keywords**

31 plugged conduit; magma mingling; slug dynamics; conduit geometry; flow configurations;
32 analogue experiments; flow modelling

33 **1. Introduction**

34 Strombolian eruptions are characterized by short impulsive events. These typically
35 occur in basaltic or andesitic magmas where viscosity is sufficiently low to allow gas
36 segregation over short time scales (Blackburn et al., 1976; Parfitt, 2004; Houghton and
37 Gonnermann, 2008). Explosions are interpreted as representing the arrival and burst of over-
38 pressured large gas pockets (slugs) at the surface (Chouet et al., 1974; Blackburn et al.,
39 1976). The slugs can form either by coalescence of smaller bubbles at geometrical
40 discontinuities in the conduit (Vergnolle and Jaupart, 1986; Jaupart and Vergnolle, 1988) or
41 by differential ascent rate of the bubbles with respect to the magma column (Parfitt and
42 Wilson, 1995; Parfitt, 2004). Either way, the ascent, expansion and burst of slugs have almost
43 always been considered in rheologically uniform media (e.g., Vergnolle and Brandeis, 1996;
44 Vergnolle et al., 1996; Seyfried and Freundt, 2000; James et al., 2006, 2008; Kobayashi et
45 al., 2010; Del Bello et al., 2012; Lane et al., 2013).

46 However, an increasing body of evidence (e.g., Lautze and Houghton, 2005, 2006;
47 Polacci et al., 2009; D’Oriano et al., 2010; Colò et al., 2010; Gurioli et al., 2014) suggests
48 that the cooling, degassing and crystallisation of the uppermost part of the magma column,
49 along with mixing with recycled material from collapses of the conduit wall, re-entrained
50 pyroclasts and lithics, could generate an evolved magma region at the top of the conduit. Gas
51 slugs must ascend and burst through this stratified rheological heterogeneity. The rheological
52 properties and thickness of this region may influence explosion intensity and style (Lautze
53 and Houghton, 2005, 2006), while textural and geochemical variations in the ejecta may
54 reflect mingling of magmas with different physical properties in the shallow conduit (Polacci

55 et al., 2009; D’Oriano et al., 2010; Colò et al., 2010; Gurioli et al., 2014). Textural features
56 observed in samples collected at Stromboli seem to correlate with explosion frequency and
57 magnitude, with a broader mingling promoted by increased magma and gas flux (i.e., greater
58 explosion frequency and vigour). In contrast, a lower flux (i.e., low level of activity) leads to
59 more restricted mingling (Lautze and Houghton, 2006). Complexities in eruptive dynamics,
60 such as pulses within a single Strombolian eruption (Taddeucci et al., 2012; Gaudin et al.,
61 2014), are also difficult to explain with simplified models of slug burst in a rheologically
62 uniform fluid, although conduit discontinuities could play a role (James et al., 2006).

63 Such evidence motivated initial experimental work on the effects of a viscous upper
64 layer (or ‘plug’) on eruptive dynamics (Del Bello et al., 2015). In this scenario, a gas slug
65 ascending and expanding in a column of low-viscosity liquid overlaid by a plug drives an
66 intrusion of low-viscosity liquid into the plug. The plug liquid thus creates a viscous annulus
67 that, in turn, encloses the intrusion (Fig. 1). As the slug arrives at the plug base, it uses the
68 low-viscosity intrusion to rise through the plug. The slug can burst in two different flow
69 configurations: 1) whilst fully accommodated into the plug volume, or 2) whilst in a low-
70 viscosity layer emplaced by the intrusion above the plug. Each configuration encompasses
71 apparent dynamic narrowing and widening of the conduit for the slug, instabilities within the
72 falling film surrounding the slug, transient partial blockages of the conduit, and slug
73 disruption (Del Bello et al. 2015). These complexities gave insight into the generation of
74 eruptive pulses and mingled pyroclasts, together with enhancement of slug overpressure with
75 respect to a single-viscosity system (Del Bello et al., 2015); however, accurate scaling for
76 slug expansion and viscosity contrast was not achieved.

77 Here, we build on the experimental foundation of Del Bello et al. (2015) to fully
78 define the rich range of fundamental fluid configurations that can develop in association with
79 slug flow through a viscous plug at the top of a volcanic conduit. We used comprehensively

80 scaled laboratory experiments to identify flow organisation and instability within different
81 fluid configurations expressed by varying relative plug and slug sizes. We developed a model
82 to determine these configurations for a given set of parameters, and validated it against the
83 laboratory data and, at volcano-scale, against the results of 3D computational fluid dynamics
84 simulations. Finally, we explored the implications of flow richness in the shallow conduit for
85 interpretation of Strombolian eruptive processes.

86 **2. Methods**

87 The complex volcanic system was simplified to explore the effect of a vertical
88 rheology contrast on the behaviour of the slug during its ascent, expansion and burst in a
89 constant-geometry tube filled with Newtonian liquids. The experimental apparatus (Fig. 1)
90 comprised a vertical 3-m-high glass tube with internal diameter D of 0.025 m. The base of the
91 tube was sealed, with the exception of the gas injection system. The top was connected to a
92 vacuum chamber in order to reduce the ambient pressure, P_a , and enable slug expansion
93 processes to be scaled (James et al., 2008). We used *AS100* silicone oil (viscosity $\mu = 0.1$ Pa
94 s, density $\rho = 990$ kg/m³, Wacker Chemie AG) as analogue for low-viscosity magma (Table
95 1), improving on the experiments of Del Bello et al. (2015) by (a) providing more accurate
96 scaling of viscosity contrast, and (b) enabling access to the explosive region of slug
97 expansion (James et al., 2009; Del Bello et al., 2012). Immiscible castor oil ($\mu = \sim 1$ Pa s, $\rho =$
98 961 kg/m³) represented the high-viscosity plug with a density less than that of the silicone oil
99 and a suitably high viscosity. At both laboratory and volcanic scales, surface tension plays a
100 negligible role (e.g., Seyfried and Freund, 2000), and the inverse viscosity N_f controls the
101 ascent of a slug:

$$102 \quad N_f = (\rho/\mu)\sqrt{gD^3} \quad (1),$$

103 where g is the gravitational acceleration. For the tube geometry, we obtain N_f values of ~ 12
104 and ~ 122 for the castor oil and silicone oil respectively (Table 1). These values lie in regions

105 of the flow regime where the slug behaviour is controlled by viscosity in the plug, and by
106 inertia with viscous contributions in the silicone oil (e.g., White and Beardmore, 1962).

107 The apparatus was filled to a height of ~ 1.43 m with either silicone oil only, or with
108 silicone oil overlain by a layer of castor oil. Layer thickness of the plug was non-
109 dimensionalised as a function of the tube diameter, D : ~ 2.5 ($1D$), ~ 5 ($2D$), ~ 12.5 ($5D$), ~ 25
110 ($10D$) and ~ 50 ($20D$) cm plugs, widening the range of Del Bello et al. (2015), which only
111 considered ~ 5 ($2D$) and ~ 17.5 ($7D$) cm layers. In addition to the gas volumes (2, 4, 6, 8 and
112 10 ± 0.1 ml) and P_a ($P_a = 3$ kPa, limited by water boiling point) used in Del Bello et al.
113 (2015), we injected volumes of air (V_0) of 17, 24, 32 and 49 ± 0.1 ml, with P_a reduced to $1 \pm$
114 0.1 kPa and 300 ± 0.1 Pa, greatly extending the range of gas expansion ratios.

115 The injected gas volumes non-dimensionalise through the parameter V_a' (Del Bello et
116 al. 2012; Supplementary Content), giving $V_a' = 0.08$ – 2 , 0.6 – 14 and 6 – 152 for experimental P_a
117 of 3 kPa, 1 kPa and 300 Pa respectively. Scaled to the volcanic case, these values represent
118 erupted gas volumes at atmospheric pressure of 4 – 90 m³, 28 – 690 m³ and 300 – 7300 m³, and
119 cover the range of gas volumes estimated for normal strombolian activity (Vergniolle and
120 Brandeis, 1996; Vergniolle et al., 1996; Ripepe and Marchetti, 2002; Chouet et al., 2003;
121 Harris and Ripepe, 2007; Mori and Burton, 2009) i.e., 2 – 2×10^4 m³ (0.5 – 3000 kg), and for
122 gas puffers, 50 – 190 m³ (10 – 30 kg). Each experiment was imaged at 300 ± 0.1 frames per
123 second with a Basler acA2000-340km high-speed camera.

124 To extend our 1D numerical model to volcanic-scale, we considered an idealised
125 system with a 200-m-high magma column within a conduit of radius 1.5, 2 or 2.5 m, covering
126 the range of values appropriate to Stromboli (Taddeucci et al., 2012; Gaudin et al., 2014).
127 Magma viscosities range between 10 – 50 kPa s and 50 – 500 Pa s, with densities of 1300 kg/m³
128 and 900 kg/m³, for the plug and the underlying magma respectively (Gurioli et al., 2014).
129 These parameters give N_f values ~ 4.55 to ~ 0.42 for the plug and ~ 630 to ~ 29 for the

130 underlying magma. Slug ascent is under dominant viscous control in the plug, but with a
131 significant degree of inertial contribution within the underlying magma, a condition
132 mimicked experimentally.

133 **3. Results**

134 The experiments revealed a rich set of flow configurations, reflecting variation in the
135 ratio of the lengths of the high-viscosity plug and gas slug. The flow configurations can be
136 conceptually considered within a spectrum of relative plug lengths, ranging from infinite (i.e.
137 a conduit fully filled with the high-viscosity liquid) to zero (i.e. a conduit filled with the low-
138 viscosity liquid). These single-viscosity end-members bracketed three distinct intermediate
139 and more complex flow configurations. The transitions between these configurations were
140 not sharp, and included intermediate behaviours. However, they encompassed the same
141 processes observed in the main configurations and, thus, are not detailed here (see
142 Supplementary Content for more information).

143 **3.1. Single viscosity**

144 We define infinitely thick and infinitely thin plugs as end-member configurations
145 (Fig. 2a, e) in which slug ascent is effectively within a single-viscosity system. In the
146 experiments, the injection of air at the base of the apparatus formed a slug (James et al., 2008;
147 Lane et al., 2013; Del Bello et al., 2015) that rose, expanded and elongated surrounded by a
148 falling liquid film. The slug burst when all the liquid head above it has flowed into the falling
149 film, except for a thin layer forming a meniscus. When ascending in a low-viscosity liquid
150 (Fig. 2e), the slug occupied almost all the cross sectional area of the tube, surrounded by a
151 thin falling film of liquid (Fig. 3); for gas volumes larger than 17 ml, film instabilities
152 developed with time. At burst, the meniscus ruptured, and its remnants were dragged upward
153 by the released gas before falling or draining back on the liquid surface (Video V01). Small
154 volumes of gas (2-8 ml) produced pre-burst oscillation of the slug nose at surface.

155 For slug ascent in high-viscosity liquids (Fig. 2a), the slug ascended with a lower
156 velocity, surrounded by a thicker falling film, thus the fraction of the tube cross-section
157 occupied by the film, A' (Del Bello et al., 2012; Supplementary Content), increased from
158 ~ 0.41 to ~ 0.52 (Table 1, Fig. 3). Consequently the area of the tube occupied by the slug
159 decreased, while its length increased. The rate of gas expansion was slower, driving a slower
160 acceleration of the liquid surface. When at the liquid surface, the slug burst with a slow
161 rupture of a thick viscous meniscus, which completely drained to the tube wall just above the
162 burst point and without the ejection of any droplets or observable pre-burst oscillation.

163 **3.2. Configuration 1**

164 In a layered system in which the plug volume was significantly greater than the slug
165 volume, a steady slug flow was established in both the low- and high-viscosity liquids (Fig.
166 2b), with a transitional period as the slug moved between the fluids (Video V02, 8-13 s). At
167 the onset of an experiment the slug rose in the low-viscosity liquid. As it ascended, gas
168 expansion drove an intrusion of low-viscosity oil into the plug, the extent of which depended
169 on the relative volumes of the slug expansion and the plug. Around the intrusion, the high-
170 viscosity liquid represented a viscous annulus, with an average radial thickness ~ 4 mm,
171 thinnest at the plug base (Fig. 3).

172 When the nose of the ascending slug reached the base of the annulus, the annulus
173 acted as a dynamic change in the confining geometry. This forced the slug to ascend through
174 a diameter reduction and into the intrusion (Fig. 4a, sketch II; Video V02, 8 s). For all
175 configurations the intrusion volume must equal the slug volume expansion; therefore the
176 intrusion was always smaller than the slug itself. Thus, at some point, the slug transited from
177 ascending within the intrusion to within the main body of the plug itself, defining
178 Configuration 1. Once this was complete, the high-viscosity plug liquid fully accommodated

179 the bubble within it (Fig. 4a, sketch III). Ascent rate and slug morphology became more
180 viscously dominated and burst processes reflected those in high-viscosity fluids (Video V02).

181 **3.3. Configuration 2**

182 For experiments in which the plug volume was insufficient to fully accommodate the
183 slug, slug burst occurred with the slug nose within the plug liquid, and the slug base still in
184 the low-viscosity liquid (Fig. 2c). As for Configuration 1, when the slug arrived at the base of
185 the annulus, it used the intrusion as a pathway through the plug (Fig. 4b, sketch II; Video
186 V03, 13-16 s) with, at some point, the slug nose entering the high-viscosity plug liquid (Fig.
187 4b, sketch III; Video V03, 16 s). At burst, the high-viscosity meniscus disrupted into small
188 droplets (Video V03, 17 s). If the nose of the intrusion had almost reached the plug surface
189 when the slug burst (mainly for $5D$ and $10D$ plugs and 10, 17 and 24 ml slugs), then the burst
190 involved droplets of a mixture of low/high viscosity oil, ejected up the tube.

191 **3.4. Configuration 3**

192 Configuration 3 represents the scenario in which slug expansion is sufficiently large
193 that the low-viscosity intrusion breaches the plug top and emplaces a layer of low-viscosity
194 liquid above the annulus (Fig. 2d; Video V04, from 5 s onwards). Experimentally, the viscous
195 annulus effectively generated two regions of geometry change for ascending slugs; at the
196 base of the plug, the annulus created a dynamic restriction, whilst at the top, slugs passed
197 back into the low-viscosity liquid only – effectively a dynamic widening (Fig. 4c, sketch II).
198 The widening enabled the slug nose to accelerate and the abrupt change led to rapid draining
199 of the liquid head around the slug (James et al., 2006). As the increased downward flux of
200 liquid past the slug nose converged at the top of the annulus, the falling film thickened within
201 the annulus, creating a narrowing neck around the slug. If this closed, the gas flow may be
202 temporarily halted as the gas slug was broken into two (Fig. 3c, sketch III; Video V04, 16-18
203 s) or, if the processes were repeated, more offspring bubbles. The break-up process, always

204 taking place in < 1 s after the main bubble burst, generated up to 4 offspring bubbles in the
205 experiments, bursting sequentially. We observed also partial restrictions of the gas escape
206 pathway, at a mean frequency of 2 per second.

207 When the slug nose within the intrusion ascended above the top of the annulus,
208 instabilities formed in the falling film around the slug body due to the dynamic geometry
209 change; these instabilities propagated down the low-viscosity film within the annulus and
210 continuously disrupted the boundary between the two liquids, initiating mingling (Fig. 4c,
211 sketch II-III). Sometimes, for large gas volumes and thin plugs (1D and 2D), gas expansion
212 caused rapid intrusion of low-viscosity liquid breaking through the plug: some of the high-
213 viscosity annulus was detached, dragged upward within the low-viscosity liquid above and
214 surrounding the slug body, and mixed into the low-viscosity liquid. As burst progressed,
215 pockets of this mingled mixture were ejected (Fig. 4c, sketch IV). The burst process was
216 highly variable: it involved bubble oscillations and detachment of the entire meniscus, or
217 bubbles burst without any oscillation, with a complete disruption of the meniscus and
218 droplets ejected high in the tube and followed by several collapses of the film lining the tube
219 wall (Video V04).

220 **4. Determination of flow configurations at volcano-scale**

221 To determine the flow configuration (e.g., 1 to 3) for a specific set of parameters, we
222 developed a first-order 1D model to describe slug ascent, expansion and intrusion of liquid
223 into the plug. The model is based on previously used geometrical representations of slug
224 morphology (Vergnolle, 1998; Seyfried and Freundt, 2000; James et al., 2008, 2009; Del
225 Bello et al., 2012) and, for simplicity, we neglected inertial forces on the liquid above the
226 slug. Such inertial effects can be important when large rates of gas expansion are involved
227 (James et al., 2008, 2009), but expansion rates will be generally reduced by the presence of
228 the plug. Thus although the model will slightly overestimate gas expansion, this

229 simplification is suitable for a model aimed only at estimating the active flow configurations.
 230 Furthermore, to retain the first-order approach and avoid the complexities involved with
 231 transitional behaviour and slug ascent within the intrusion, the model determines the active
 232 configuration no later than the point at which the slug nose reached the original plug base,
 233 without considering the full ascent up to slug burst.

234 The slug is represented as a cylinder of length L and constant radius r_s , ascending in a
 235 vertical tube of radius r_c (Fig. 5, Table 2 for notation). Above the slug, we consider three
 236 different sections; the lowest filled by the low-viscosity liquid only, viscosity μ_1 and density
 237 ρ_1 , of height h_1 . The uppermost section represents the viscous plug, with viscosity μ_2 , density
 238 ρ_2 , radius r_c and height h_3 . The middle section represents the intrusion of low-viscosity liquid
 239 into the high-viscosity plug to form the annulus, with viscosity μ_1 and density ρ_1 , length h_2
 240 and radius r_ϕ . The radius r_ϕ is the result of $r_\phi = r_c - r_p$, where r_p is the thickness of the high-
 241 viscosity layer against the tube wall which forms the high-viscosity annulus. Due to the
 242 evolving nature of the annulus, r_p will vary in space and time. Consequently, in order to
 243 provide a characteristic first-order estimate in our straightforward model we assume a
 244 thickness as for a falling film surrounding a slug, which can be given as a function of the
 245 inverse viscosity, N_f (Llewellyn et al., 2012; Supplementary Content):

$$246 \quad r_p = (0.204 + 0.123 \tanh(2.66 - 1.15 \log_{10} N_f)) r_c \quad (2).$$

247 Initial conditions are the height of the low-viscosity liquid above the slug nose, h'_1 , the
 248 height of the plug, h'_3 , the initial (magnastatic) bubble pressure, $P_0 = \rho g(h'_1 + h'_3) + P_a$, the
 249 slug length, L_0 , and radius, $r_s = r_c - \lambda$, where λ is the thickness of the low-viscosity falling
 250 liquid film, determined by using equation (2) for the low-viscosity liquid (Fig. 3).

251 We assume constant velocity v_s for the slug base, thus, at any time, t , the height of the
 252 low-viscosity liquid column h_1 above the slug nose is given by:

$$253 \quad h_1 = (L_0 - L) - v_s t + h'_1 \quad (3).$$

254 Equating the intrusion volume to the gas expansion, the height of the low-viscosity liquid
255 intrusion h_2 can be expressed as:

$$256 \quad h_2 = -A(L_0 - L) \quad (4),$$

257 where $A = \frac{r_s^2}{r_\phi^2}$. Conservation of volume for the plug liquid yields:

$$258 \quad \pi r_c^2(h_3 + h_2) - \pi r_\phi^2 h_2 = \pi r_c^2 h'_3 \quad (5),$$

259 where h_3 is the distance between the plug top and the intrusion (h_2) top. Simplifying and
260 substituting for h_2 , h_3 can be expressed as:

$$261 \quad h_3 = h'_3 + (L_0 - L)(A - B) \quad (6),$$

262 where $B = \frac{r_s^2}{r_c^2}$.

263 The force on the liquid column above the slug due to the pressure difference between
264 the slug and the surface is given by $F_p = \pi r_s^2(P - P_\alpha)$. If the slug behaves like a perfect gas
265 and adiabatic expansion, then $PV^\gamma = \text{constant}$ (where γ is the ratio of specific heat), and the
266 slug pressure, with constant radius and pressure P_0 at $t = 0$, F_p can be expressed as:

$$267 \quad F_p = \pi r_s^2(P_0 L_0^\gamma L^{-\gamma} - P_\alpha) \quad (7).$$

268 The gravitational force is given by $F_g = -\pi r_s^2 \rho h g$, where ρ and h are respectively
269 the density and the height of the involved liquid, and g is the acceleration due to gravity.
270 Finally, assuming no-slip conditions at the wall, the Poiseuille law gives the viscous force for
271 a laminar flow in a cylindrical pipe:

$$272 \quad F_v = -8\pi\mu h V_f \quad (8),$$

273 where μ is the viscosity of the liquid and V_f the flow velocity. If we assume that the liquid
274 flow is equal to the volume flux controlled by the gas expansion, we obtain:

$$275 \quad F_v = -8\pi\mu h \dot{L} B \quad (9).$$

276 Equating the pressure force with the sum of the gravitational and viscous forces for the low-
 277 viscosity liquid column above the slug, the low-viscosity liquid intrusion, and the plug, we
 278 obtain:

$$279 \quad \pi r_s^2 (P_0 L_0^\gamma L^{-\gamma} - P_a) = -\pi r_s^2 \rho_1 g (h_1 + h_2) - \pi r_s^2 \rho_2 g h_3 - 8\pi \dot{L} \frac{r_s^2}{r_c^2} (\mu_1 h_1 + \mu_2 h_3) -$$

$$280 \quad 8\pi \dot{L} \frac{r_\phi^2}{r_c^2} \mu_1 h_2 \quad (10).$$

281 Simplifying and substituting for both h_2 and h_3 yields:

$$282 \quad (P_0 L_0^\gamma L^{-\gamma} - P_a) =$$

$$283 \quad -g[\rho_1 (h_1 - A(L_0 - L))] - g[\rho_2 (h'_3 + (L_0 - L)(A - B))] - 8\dot{L} r_c^{-2} [\mu_1 h_1 + \mu_2 [h'_3 +$$

$$284 \quad (L_0 - L)(A - B)]] - 8\dot{L} r_\phi^2 \frac{r_c^{-2}}{r_s^2} \mu_1 [-A(L_0 - L)] \quad (11),$$

285 and finally:

$$286 \quad \dot{L} = \{-g[\rho_1 (h_1 - A(L_0 - L))] - g[\rho_2 (h'_3 + (L_0 - L)(A - B))] + (P_0 L_0^\gamma L^{-\gamma} -$$

$$287 \quad P_a)\} / \{8r_c^{-2} [\mu_1 h_1 + \mu_2 [h'_3 + (L_0 - L)(A - B)]] + 8r_\phi^2 \frac{r_c^{-2}}{r_s^2} \mu_1 [-A(L_0 - L)]\} \quad (12).$$

288 The first order differential is solved numerically in *Matlab*, using a Runge-Kutta
 289 formula. With the focus of the model being to determine flow configurations within the
 290 parameter space of a system, it is sufficient to consider the values determined when either the
 291 intrusion breaches the plug surface, $h_3 = 0$ (indicating Configuration 3) or when the slug
 292 reaches the plug base, $h_1 = 0$. In this latter case, Configuration 1 is identified if there is
 293 sufficient plug material to fully encompass the volume of the gas slug, otherwise
 294 Configuration 2 is determined.

295 4.1. Model validation

296 To verify the suitability of equation (12), we compared modelled slug ascent to
 297 experimental data representative of each configuration (Fig. 6). For model inputs, we
 298 measured the ascent velocity of the base from the laboratory video, derived the initial slug

299 length directly from the experimental gas volumes, and, to calculate the intrusion radius,
300 assumed the value of the annulus radius equal to a falling film surrounding a slug. For
301 Configuration 1 (Fig. 6a) and 2 (Fig. 6b), the model accurately reproduced the variations in
302 position of the slug nose, base and the liquid surface, with the intrusion level always below
303 the plug surface. For Configuration 3 (Fig. 6c), the model accurately predicted both the
304 timing and position of the plug breach.

305 We neglected the inertial forces in the formulation of equation (12), so gas expansion
306 is slightly overestimated by the model, as well as the intrusion volume, leading to small
307 discrepancies between the laboratory experiments and model results (Fig. 7a). Larger slugs
308 and rapid gas expansion, resulting in greater intrusion of low-viscosity liquid, cause the
309 model prediction of Configuration 3 or 2 instead of Configuration 2 or 1 respectively.
310 However, when compared to the experimental data and considering the simplifying
311 assumptions, the model successfully identifies the dominant areas of parameter space for
312 Configuration 1 and 3, separated by Configuration 2.

313 Applying the model to an idealised volcanic-scale scenario (Fig. 7b) indicated that a
314 similar pattern of flow configurations could be relevant at Stromboli. To corroborate this, we
315 carried out 3D computational fluid dynamics (CFD) simulations using the commercial
316 software Flow3D (James et al., 2008; Chouet et al., 2010; Del Bello et al., 2015).

317 First, we modelled selected laboratory experiments to validate the CFD model against
318 experimental data, recreating the same experimental conditions (apparatus geometry, injected
319 slug volumes, experimental ambient pressures and plug thickness). The CFD simulations
320 produced results similar to those observed in the laboratory in terms of both flow processes
321 and slug and intrusion shapes (Fig. 8a, b; Video V05). The generation of the viscous annulus
322 and the complex interaction between the two liquids were also accurately reproduced,

323 together with the disruption of the slug and the generation of offspring bubbles and partial
324 blockages of the conduit (fig. 8c, d; Video V05).

325 For the volcanic scenario, a 300-m-high vertical cylinder with a radius of 1.5 m (for
326 CFD simulations, only this conduit radius was used), closed at the lower boundary,
327 represented the conduit. Although a closed condition was not realistic and more
328 representative of the experimental condition, once a stable slug flow was established in the
329 conduit, this boundary condition did not affect the flow (e.g., James et al., 2008; Chouet et
330 al., 2010). The 200-m-high magma column was modelled as an incompressible Newtonian
331 liquid with a temperature-dependent viscosity and divided into two temperature regions. The
332 first region covered the low-viscosity magma, while the second region defined the plug.
333 Viscosity values ranged between 10-1000 Pa s for the magma beneath the plug and between
334 1-20 kPa s for the plug, lower than the typical value of Stromboli (1-50 kPa s, Gurioli et al.,
335 2014): exceeding that range resulted in simulation initialisation problems. The gas slug was
336 modelled as a continuous void region (contains no mass) governed by the equation $PV^n =$
337 *constant*.

338 The volcano-scale simulations, for plug thickness and gas volumes of 3–60 m and 30–
339 250 m³ respectively, showed changes in slug shape as it enters the annulus (Fig. 8e, f), and
340 reproduced the generation of instabilities and slug disruption (Fig. 8g-l). As predicted, the
341 slug transition from a low-viscosity magma to a viscous plug caused a sudden decrease in the
342 slug ascent velocity. As for the burst process, different dynamics can be associated with the
343 different configurations. Based purely on visual observation of the burst dynamics,
344 Configuration 1 involved a slow fragmentation of the viscous meniscus above the slug, with
345 almost no pyroclast ejection. In Configuration 2 the fragmentation of the magma meniscus
346 was fast and its particles were ejected up to tens of meters above the burst point (note this is a
347 minimum inertial height since no drag from expanding gas is applied). Configuration 3

348 explosions ranged in style depending on slug volumes, plug thickness, generation of
349 secondary bubbles and blockages of the conduit. In general the burst process seemed
350 characterized by dynamics common to both Configuration 1 and 2, with ejection of material
351 above the burst point but at heights inferior to Configuration 2. Furthermore, most of the
352 ejecta appeared to be mingled and collapsed back in the conduit, creating partial blockages
353 that forced the slug into smaller pockets of gas.

354 The simulations, showing flow processes similar to those observed in the scaled
355 laboratory experiments, support the applicability of the 1D model and endorse the main roles
356 played by slug volume and plug properties in determining the prevailing flow configuration.
357 The computational fluid dynamics simulations also enabled investigation of the role of the
358 underlying magma viscosity on the complex syn- and post-burst dynamics involved in
359 Configuration 3. A lower viscosity magma drained faster along the conduit/annulus walls,
360 accumulating at the top of the annulus. This promoted the fast and cyclic creation of
361 narrowing necks around the slug. Every time a neck closed, the slug was disrupted,
362 generating offspring bubbles and secondary bursts (pulses). Magma clots were also ejected at
363 greater heights and their collapse produced partial blockages of the conduit, trapping the slug
364 gas into smaller pockets and leading to sub-pulses. For each pulse and sub-pulse, burst depth
365 gradually increased (Video V06, 21-34 s). With increasing magma viscosity, drainage along
366 the conduit walls slowed, with the generation of fewer, or no, pulses but only partial
367 blockages due to collapse of material back into the conduit (Video V06).

368 **5. Implications for Strombolian eruptions**

369 Our experiments characterised the spectrum of flow configurations for a set of liquid
370 parameters, tube geometry and for single slug ascent in a rheologically stratified conduit. In
371 our idealised volcanic scenario, both configuration model and CFD simulations indicate the
372 sensitivity of configurations to initial gas volumes and plug properties (Fig. 7b). For a

373 particular conduit radius, the distribution of configurations in parameter space was insensitive
374 to the viscosity of the magma beneath the plug, which can be considered mainly as a means
375 of delivering the slug into the plug (Fig. 7b, Video V06). In contrast, conduit radius had a
376 strong influence on configuration transitions. The Configuration 1 domain increased with
377 increasing radius (Fig. 7b) implying that, for identical magmatic conditions, vents of different
378 radius could erupt with different style.

379 Under plugged conditions, it appeared both experimentally and numerically that the
380 burst vigour was always greater when compared to an unplugged scenario. As previous
381 models in single-viscosity systems demonstrated, slug overpressure varies with the thickness
382 of the falling film, controlled by magma viscosity (James et al., 2009; Del Bello et al., 2012).
383 Hence, the same initial gas volume burst with a lower overpressure in a low-viscosity liquid
384 (thin film, Fig. 2e) compared to in a higher viscosity liquid (thick film, Fig. 2a). This effect
385 occurred in Configuration 1; however, because the slug was initially ascending in a low-
386 viscosity magma, its overpressure also increased due to pressurization of the conduit below
387 the plug. The greater the plug thickness and viscosity, the more pressure can be retained to be
388 released during a more vigorous burst.

389 Within Configuration 2, gas expansion intruded a substantial volume of low-viscosity
390 liquid into the plug; the further the intrusion penetrated, the higher the slug can ascend within
391 the low-viscosity channel enclosed within the viscous annulus. The greater thickness of the
392 complex “double” falling film resulted in increased slug lengthening to accommodate gas
393 expansion, opposed by the presence of the un-intruded plug above, and enhancing the
394 generation of overpressure. In Configuration 3, the full development of an open low-viscosity
395 channel through the plug removed the ‘capping’ effect, allowing the slug to expand more
396 freely and, compared to the other two configurations, reducing slug overpressure.

397 Furthermore, the partial constriction of the tube and the gas slug break-up into smaller
398 pockets produced multiple bursts and modulation of the gas release within Configuration 3.

399 In support of the role of different flow configurations on slug overpressure, Del Bello
400 et al. (2015) quantified similar effects for their experiments, that can be now categorised as
401 Configurations 1 and 3 (Configuration 2 was not identified). All of their plugged
402 experiments, regardless plug thickness, showed a greater acoustic amplitude and an increase
403 in slug overpressure with respect to the single-viscosity experiments (Fig. 3 and 4 in Del
404 Bello et al. 2015). In Configuration 1, Del Bello et al's slugs showed a greater increase in
405 both conduit pressurization during slug ascent and acoustic amplitude at burst compared to
406 slugs bursting in Configuration 3. In Configuration 3, slugs were characterized by a lower
407 overpressure but also by highly variable gas release rates, both in terms of magnitude and
408 time, and generated a range of pressure pulses (burst of offspring bubbles) and sub-pulses
409 (conduit constriction) (Del Bello et al. 2015).

410 Therefore, for volcanoes where multiple vents are constantly active (e.g., Stromboli
411 and Yasur, Vanuatu), each active vent may be characterized by plugs with different
412 properties, controlling both burst dynamics and explosion magnitude, thus affecting acoustic
413 amplitudes. However, a unique explanation of a particular acoustic amplitude is further
414 complicated because the same gas mass can lead to different flow configurations sensitive to
415 conduit width (Fig. 7b). Slug parameterization and the linking of field results and fluid
416 dynamic models, so far based on single-viscosity scenarios suggesting a positive correlation
417 for the burst pressure with both initial slug volume and magma viscosity (e.g., Vergnolle and
418 Brandeis 1996; James et al., 2009; Del Bello et al., 2012; Lane et al., 2013), becomes more
419 poorly constrained with the added degrees of freedom provided by rheological complexity.

420 **5.1. Magma mingling**

421 As a result of interactions between the different viscosity magmas, the textural and
422 geochemical properties of the ejected pyroclasts will also depend on the flow processes
423 occurring within the plug. Our experiments reveal that mingling of material may occur in two
424 ways. If the low-viscosity magma intrudes the plug deep enough but without breaching it, the
425 slug approaches the surface surrounded by a low-viscosity magma film, enclosed in turn by
426 the high-viscosity annulus forming a tri-axial flow (Del Bello et al., 2015), i.e., at the
427 boundary of Configuration 2 with 3. At burst, the fragmenting meniscus will comprise layers
428 of both low- and high-viscosity magma, promoting mingling and ejection of mingled
429 pyroclasts. However, with only the meniscus region involved, mingling is expected to be a
430 relatively localized process. A more extended mingling occurs within Configuration 3 (Fig.
431 2d and 4c), where: (a) globules of the annulus are mixed into the low-viscosity liquid during
432 rapid intrusion and (b) flow instabilities (also observed by Del Bello et al., 2015) produce
433 cyclic collapses of the low-viscosity film which, in turn, initiate a broader mingling with the
434 high-viscosity liquid of the annulus within the tri-axial flow. The same instabilities are
435 responsible for slug break-up and for creating partial blockages in the conduit that force the
436 slug into smaller pockets. The effect is a pulsatory bursting with these processes coexisting.
437 Both laboratory observations (Video V04, V07) and, particularly, CFD simulations for
438 Stromboli (Video V06) showed that the secondary burst depths changed with time. Initially,
439 the slug burst in the low-viscosity magma above the plug. Slug break-up then occurred at the
440 top of the viscous annulus and secondary bubbles and transient gas pockets burst inside a
441 region of mingled material or within the plug, with the burst depth gradually increasing.
442 Ejected material was, therefore, scavenged at increasing depth with time, sampling different
443 regions of the complex collapsing liquid structure. Physical changes in magma should then
444 occur at two different scales, and the level of mingling could help in determining the flow

445 configurations. If mixing occurs mainly during slug ascent (Configuration 3), mingling is a
446 predominant process, likely showing, e.g., the coexistence of different vesicle populations. In
447 contrast, the lower the mingling in the ejecta, the more restricted is the process, reflecting a
448 possible mingling only at burst, during magma fragmentation (Configuration 2). Analysis of
449 the mingling textures within ejecta from a strombolian eruption could, therefore, provide
450 evidence of the near-surface flow dynamics within the conduit.

451 **5.2. Pulsatory behaviour**

452 At Stromboli, Gaudin et al. (2014) related individual pyroclast ejection pulses to
453 successive pressure release pulses and sub-pulses of duration between 0.05–2 s and an
454 average pulse rate of 7 per second, with a minimum of 3 up to 120 pulses per eruption. As a
455 general trend, with some exceptions, the greater the number of pulses and sub-pulses, the
456 longer the explosions, with greater gas masses involved (Gaudin et al., 2014). In our
457 experiments, secondary bursts (pulses), followed by several partial blockages (sub-pulses) of
458 the gas path, were achieved only in Configuration 3, with their larger number resulting from
459 the disruption of larger gas volumes (24–49 ml). Smaller volumes (8–17 ml) generated
460 offspring bubbles, without any sub-pulses, and shorter burst times. With these volumes scaled
461 to the volcanic-case, CFD simulations showed the same positive correlation between volumes
462 and number of pulses and sub-pulses as measured in the experiments. Although no formal
463 scaling exists for these processes at laboratory-scale, the trend observed in both laboratory
464 and CFD simulations is similar to the one derived from field observations, also suggesting the
465 presence of a plug as a pre-requisite for pulsatory behaviour. Furthermore, CFD simulations
466 showed that greater initial gas volume and lower viscosity of the underlying magma favour
467 secondary bursts from offspring bubbles and sub-pulses generated by partial blockages of the
468 conduit, while a higher viscosity led mainly to sub-pulses (restriction of gas escape pathway),
469 with the generation of fewer, or no, secondary bubbles (blockage of gas escape pathway;

470 Video V06). Hence, while not measurably affecting the pre-burst processes, the viscosity of
471 the underlying magma can noticeably influence syn-and post-burst dynamics and therefore
472 any measured geophysical signals.

473 **6. Conclusions**

474 Based on scaled laboratory experiments we define a framework to describe the
475 characteristic styles of the flow organisation involved with the ascent and burst of slugs in a
476 rheologically stratified conduit, where a high-viscosity plug overlies a low-viscosity magma.
477 Conduits that are fully filled with either high- or low-viscosity magma represent end-member
478 scenarios that can be considered as infinitely thick or thin high-viscosity plugs respectively.
479 In between, our experiments demonstrated three fundamental flow configurations,
480 determined by the ratio of plug size and slug gas volume. In Configuration 1, the plug was
481 sufficiently large to fully accommodate the ascending slug. In Configuration 2, a smaller plug
482 was sufficient to accommodate the volume change due to expansion of the slug on ascent, but
483 not the full volume of the slug. Consequently, when the slug burst at the surface of the plug,
484 its base was still in the low-viscosity liquid. Finally, in Configuration 3, slug expansion drove
485 an intrusion of low-viscosity liquid right through the plug, enabling slug burst to occur within
486 the low-viscosity liquid, with the plug acting only as a region of effectively reduced conduit
487 diameter.

488 We developed a model, validated with the laboratory experiments and by 3D CFD
489 simulations at volcano-scale, to explore configuration parameter space. Our results showed
490 how gas volume, plug thickness and plug viscosity were the key parameters controlling the
491 transitions between different configurations; transitions were much less sensitive to properties
492 of the underlying magma. Each configuration encompassed a variety of processes: dynamic
493 narrowing and widening of the effective conduit, generation of instabilities along the falling
494 liquid film, transient blockages of the slug path and slug break-up. These complexities

495 influenced the slug ascent dynamics and gas overpressure at burst, and thus also the resulting
496 eruptive style and, by implication, geophysical signals.

497 The complex flow processes can also promote magma mingling, not only by
498 fragmentation of a rheologically layered meniscus but also through instabilities in the falling
499 film and surrounding fluid annulus, leading to more localized or distributed regions of
500 mingling respectively. In Configuration 3, flow instabilities cause a narrowing of the gas
501 escape pathway causing sub-pulses within the eruption process. The flow instabilities can be
502 sufficient to seal the gas escape pathway and cause slug break-up through the creation of
503 transient blockages, resulting in a pulsatory, multi-bubble burst process. A widening of the
504 conduit was needed for the slug break-up and falling film collapses, and both the viscosity of
505 the underlying magma and the gas volume seemed to determine the frequency of pulses and
506 sub pluses.

507 Our results showed how these flow configurations can influence eruption vigour, style
508 and pyroclast properties. The configuration framework should be considered when
509 interpreting slug-burst related geophysical signals, and points the way to more detailed links
510 between fluid dynamic models and acoustic signals.

511 **7. Video description**

512 Videos **V01**, **V02**, **V03** and **V04** show the flow processes occurring during slug ascent,
513 expansion and burst in the following experiments: (**V01**) Single and low-viscosity system,
514 plug $h = 0$ cm ($0D$), $P_a = 1$ kPa, $V_0 = 6$ ml; (**V02**) Configuration 1, plug $h = 50$ cm ($20D$), $P_a =$
515 1 kPa, $V_0 = 6$ ml; (**V03**) Configuration 2, plug $h = 12.5$ cm ($5D$), $P_a = 1$ kPa, $V_0 = 6$ ml. (**V04**)
516 Configuration 3, plug $h = 12.5$ cm ($5D$), $P_a = 300$ Pa, $V_0 = 49$ ml. Video **V05** shows the
517 comparison between a laboratory experiment and a CFD simulation for a 10 ml slug, $P_a = 3$
518 kPa and plug $h = 5$ cm ($2D$); frame rate of the laboratory video has been accelerated to allow
519 an easier video comparison. Video **V06** shows the comparison between three different CFD

520 simulations at volcanic-scale, for the same gas volume, $V_0 = 140 \text{ m}^3$, ascending in a 300-m-
521 high volcanic conduit of radius 1.5 m, filled with magma beneath the plug (plug $h = 15 \text{ m}$
522 [5D]) of viscosities 50 (left), 150 (middle) and 300 (right) Pa s. Video **V07** contains a
523 sequence of the bubble break-up process from an experiment of a 24 ml slug, $P_a = 3 \text{ kPa}$ and
524 plug $h = 12.5 \text{ cm}$ (5D).

525 **8. Acknowledgments**

526 This research is part of A.C. PhD at Lancaster University, funded by the People Programme
527 (Marie Curie Actions) of the European Union's Seventh Framework Programme (FP7/2007-
528 2013) under the project NEMOH, REA grant agreement n° 289976. We thank Kathy
529 Cashman and Sylvie Vergnolle for thorough and constructive comments that greatly
530 improved the manuscript, and the editor Bernard Marty.

531

532 **References**

533 Blackburn, E.A., Wilson, L., and Sparks, R.S.J., 1976, Mechanisms and dynamics of
534 strombolian activity. *Journal of the Geological Society*, v. 132, no. 4, p. 429–440, doi:
535 10.1144/gsjgs.132.4.0429.

536 Chouet, B., Hamisevicz, N., and Mcgetchin, T.R., 1974, Photoballistics of Volcanic Jet
537 Activity at Stromboli, Italy. *J. Geophys. Res.*, v. 79, no. 32, p. 4961–4976.

538 Chouet, B., P. Dawson, Ohminato, T., Martini, M., Saccorotti, G., Giudicepietro, F., De
539 Luca, G., Milana, G., and Scarpa, R., 2003, Source mechanisms of explosions at Stromboli
540 Volcano, Italy, determined from moment-tensor inversions of very-long-period data. *J.*
541 *Geophys. Res.*, 108(B1), 2019, doi:10.1029/2002JB001919.

542 Chouet, B., Dawson, P., Martini, M., 2008. Shallow-conduit dynamics at Stromboli Volcano,
543 Italy, imaged from waveform inversions. In: Lane, S.J., Gilbert, J.S. (Eds.), *Fluid Motions in*
544 *Volcanic Conduits: A Source of Seismic and Acoustic Signals: Geol. Soc., London, Special*
545 *Publications*, 307, pp. 57–84.

546 Chouet, B. A., P. B. Dawson, M. R. James, and S. J. Lane, 2010, Seismic source mechanism
547 of degassing bursts at Kilauea Volcano, Hawaii: Results from waveform inversion in the 10–
548 50 s band. *J. Geophys. Res.*, v. 115, B09311, doi:10.1029/2009JB006661.

549 Colò, L., Ripepe, M., Baker, D.R., and Polacci, M., 2010, Magma vesiculation and infrasonic
550 activity at Stromboli open conduit volcano. *Earth Planet. Sci. Lett.*, v. 292, no. 3-4, p. 274–
551 280, doi: 10.1016/j.epsl.2010.01.018.

552 D’Oriano, C., Bertagnini, A., and Pompilio, M., 2011, Ash erupted during normal activity at
553 Stromboli (Aeolian Islands, Italy) raises questions on how the feeding system works. *Bull.*
554 *Volcanol.*, v. 73, no. 5, p. 471–477, doi: 10.1007/s00445-010-0425-0.

555 Del Bello, E., Llewellyn, E.W., Taddeucci, J., Scarlato, P., and Lane, S.J., 2012, An analytical
556 model for gas overpressure in slug-driven explosions: Insights into Strombolian volcanic
557 eruptions. *J. Geophys. Res.*, v. 117, no. B2, p. B02206, doi: 10.1029/2011JB008747.

558 Del Bello, E., Lane, S.J., James, M.R., Llewellyn, E.W., Taddeucci, J., Scarlato, P., Capponi,
559 A., 2015, Viscous plugging can enhance and modulate explosivity of strombolian eruptions.

560 Earth Planet. Sci. Lett., v. 423, 1 August 2015, p. 210-218, ISSN 0012-821X,
561 <http://dx.doi.org/10.1016/j.epsl.2015.04.034>.

562 Gaudin, D., Taddeucci, J., Scarlato, P., Moroni, M., Freda, C., Gaeta, M., and Palladino,
563 D.M., 2014, Pyroclast Tracking Velocimetry illuminates bomb ejection and explosion
564 dynamics at Stromboli (Italy) and Yasur (Vanuatu) volcanoes. *J. Geophys. Res.*, v. 119, no.
565 7, p. 5384–5397, doi: 10.1002/2014JB011096.

566 Gurioli, L., Colò, L., Bollasina, A.J., Harris, A.J.L., Whittington, A., and Ripepe, M., 2014,
567 Dynamics of strombolian explosions: inferences from field and laboratory studies of erupted
568 bombs from Stromboli volcano. *J. Geophys. Res.*, v. 119, 319–345,
569 doi:10.1002/2013JB010355.

570 Harris, A., and M. Ripepe, 2007, Temperature and dynamics of degassing at Stromboli. *J.*
571 *Geophys. Res.*, 112, B03205, doi:10.1029/2006JB004393.

572 Houghton, B.F., Gonnermann, H.M., 2008, Basaltic explosive volcanism: Constraints from
573 deposits and models. *Chemie der Erde - Geochemistry*, v. 68, Issue 2, 117-140, ISSN 0009-
574 2819, <http://dx.doi.org/10.1016/j.chemer.2008.04.002>.

575 James, M.R., Lane, S.J., and Chouet, B.A., 2006, Gas slug ascent through changes in conduit
576 diameter: Laboratory insights into a volcano-seismic source process in low-viscosity
577 magmas. *J. Geophys. Res.*, v. 111, no. B5, p. B05201, doi: 10.1029/2005JB003718.

578 James, M.R., Lane, S.J., and Corder, S.B., 2008, Modelling the rapid near-surface expansion
579 of gas slugs in low viscosity magmas. *Geological Society, London, Special Publications*, v.
580 307, no. 1, p. 147–167, doi: 10.1144/SP307.9.

581 James, M.R., Lane, S.J., Wilson, L., and Corder, S.B., 2009, Degassing at low magma-
582 viscosity volcanoes: Quantifying the transition between passive bubble-burst and
583 Strombolian eruption. *J. Volcanol. Geotherm. Res.*, v. 180, no. 2-4, p. 81–88, doi:
584 10.1016/j.jvolgeores.2008.09.002.

585 Jaupart, C., and Vergnolle, S., 1988, Laboratory models of Hawaiian and Strombolian
586 eruptions. *Nature*, 331, 6151, 58-60

587 Kobayashi, T., Namiki, A., and Sumita, I., 2010, Excitation of airwaves caused by bubble
588 bursting in a cylindrical conduit: Experiments and a model. *J. Geophys. Res.*, doi:
589 10.1029/2009JB006828.

590 Lane, S.J., James, M.R., and Corder, S.B., 2013, Volcano infrasonic signals and magma
591 degassing: First-order experimental insights and application to Stromboli. *Earth Planet. Sci.*
592 *Lett.*, v. 377-378, p. 169–179, doi: 10.1016/j.epsl.2013.06.048.

593 Lautze, N.C., and Houghton, B.F., 2005, Physical mingling of magma and complex eruption
594 dynamics in the shallow conduit at Stromboli volcano, Italy. *Geology*, v. 33, no. 5, p. 425,
595 doi: 10.1130/G21325.1.

596 Lautze, N.C., and Houghton, B.F., 2006, Linking variable explosion style and magma
597 textures during 2002 at Stromboli volcano, Italy. *Bull. Volcanol.*, v. 69, no. 4, p. 445–460,
598 doi: 10.1007/s00445-006-0086-1.

599 Llewellyn, E.W., Del Bello, E., Taddeucci, J., Scarlato, P., and Lane, S.J., 2012, The
600 thickness of the falling film of liquid around a Taylor bubble. *Proc. R. Soc., Math. Phys. Eng.*
601 *Sci.*, v. 468, no. 2140, p. 1041–1064, doi: 10.1098/rspa.2011.0476.

602 McGreger, A.D., and Lees, J.M. 2004, Vent discrimination at Stromboli volcano, Italy. *J.*
603 *Volcanol. Geotherm. Res.*, v. 137, 169–185, doi:
604 <http://dx.doi.org/10.1016/j.jvolgeores.2004.05.007>.

605 Mori, T., and Burton, M., 2009, Quantification of the gas mass emitted during single
606 explosions on Stromboli with the SO₂ imaging camera. *J. Volcanol. Geotherm. Res.*, 188(4),
607 395-400, doi:10.1016/j.jvolgeores.2009.10.005

608 Parfitt, E.A., and Wilson, L., 1995, Explosive volcanic eruptios: IX The transition between
609 Hawaiian-style lava fountaining and Strombolian explosive activity. *Geophys. J. Int.*, 121,
610 226-232

611 Parfitt, E. A., 2004, A discussion of the mechanisms of explosive basaltic eruptions. *Journal*
612 *of Volcanology and Geothermal Research*, 134(1–2), 77–107,
613 doi:10.1016/j.jvolgeores.2004.01.002.

614 Polacci, M., Baker, D. R., Mancini, L., Favretto, S., and Hill, R.J., 2009, Vesiculation in
615 magmas from Stromboli and implications for normal Strombolian activity and paroxysmal
616 explosions in basaltic systems. *J. Geophys. Res.*, v. 114, B01206, doi:
617 10.1029/2008JB005672.

618 Ripepe, M., and Marchetti, E., 2002, Array tracking of infrasonic sources at Stromboli
619 volcano. *Geophys. Res. Lett.*, 29(22), 33-1. doi: 10.1029/2002GL015452

620 Seyfried, R., and Freundt, A., 2000, Experiments on conduit flow and eruption behaviour of
621 basaltic volcanic eruptions. *J. Geophys. Res.*, v. 105, no. B10, p. 727-740, doi:
622 10.1029/2000JB900096.

623 Taddeucci, J., Scarlato, P., Capponi, A., Del Bello, E., Cimarelli, C., Palladino, D.M., and
624 Kueppers, U., 2012, High-speed imaging of Strombolian explosions: The ejection velocity of
625 pyroclasts. *Geophys. Res. Lett.*, v. 39, no. 2, L02301, doi: 10.1029/2011GL050404.

626 Vergnolle, S., and Jaupart, C., 1986, Separated two-phase flow and basaltic eruptions. *J.*
627 *Geophys. Res.*, 91(B12), 12842-12860.

628 Vergnolle, S., and Brandeis, G., 1996, Strombolian explosions 1. A large bubble breaking at
629 the surface of a lava column as a source of sound. *J. Geophys. Res.*, v. 101, no. B9, p. 433–
630 447.

631 Vergnolle, S., Brandeis, G., and Mareschal, J.C., 1996, Strombolian explosions 2. Eruption
632 dynamics determined from acoustic measurements. *J. Geophys. Res.*, v. 101, no. B9, p. 449–
633 466.

634 Vergnolle, S., 1998, Modelling two-phase flow in a volcano. In *Proc. 13th Australasian*
635 *Fluid Mech. Conf. Aristoc. Offset, Monash University, Melbourne*, 647-650.

636 White, E. T., and Beardmore, R. H., 1962, The velocity of rise of single cylindrical air
637 bubbles through liquids contained in vertical tubes. *Chem. Eng. Sci.*, v. 17, p. 351–361.

638

639 **Table 1** Comparison of experimental parameters from this study and from Del Bello et al. (2015) and
 640 scaling to the volcanic case

Materials	Water ^a	Silicone oil ^b	Castor oil ^{a-b}	Underlying magma ^e	Plug ^e
Conduit radius, r_c (m)		0.0125		2.5	
Density (kg/m³)	1000	990	961	900	1300
Viscosity (Pa s)	0.001	0.1	1	50-300	10000-50000
Inverse viscosity, N_f	12380	122	12	630-105	4.5-0.91
Film cross section, A'^c	0.16	0.41	0.52	0.26-0.36	0.53-0.54
Dimensionless film, λ'^d	0.08	0.23	0.31	0.14-0.24	0.32-0.32
Film thickness, λ (m)	0.001	0.0029	0.0039	0.35-0.60	0.80-0.81
Slug radius, r_s (m)	0.011	0.0095	0.0085	1.89-2.14	1.67-1.68
Viscosity contrast	1000	10		33-1000	

641 ^a used in Del Bello et al. (2015)

642 ^b used in this study

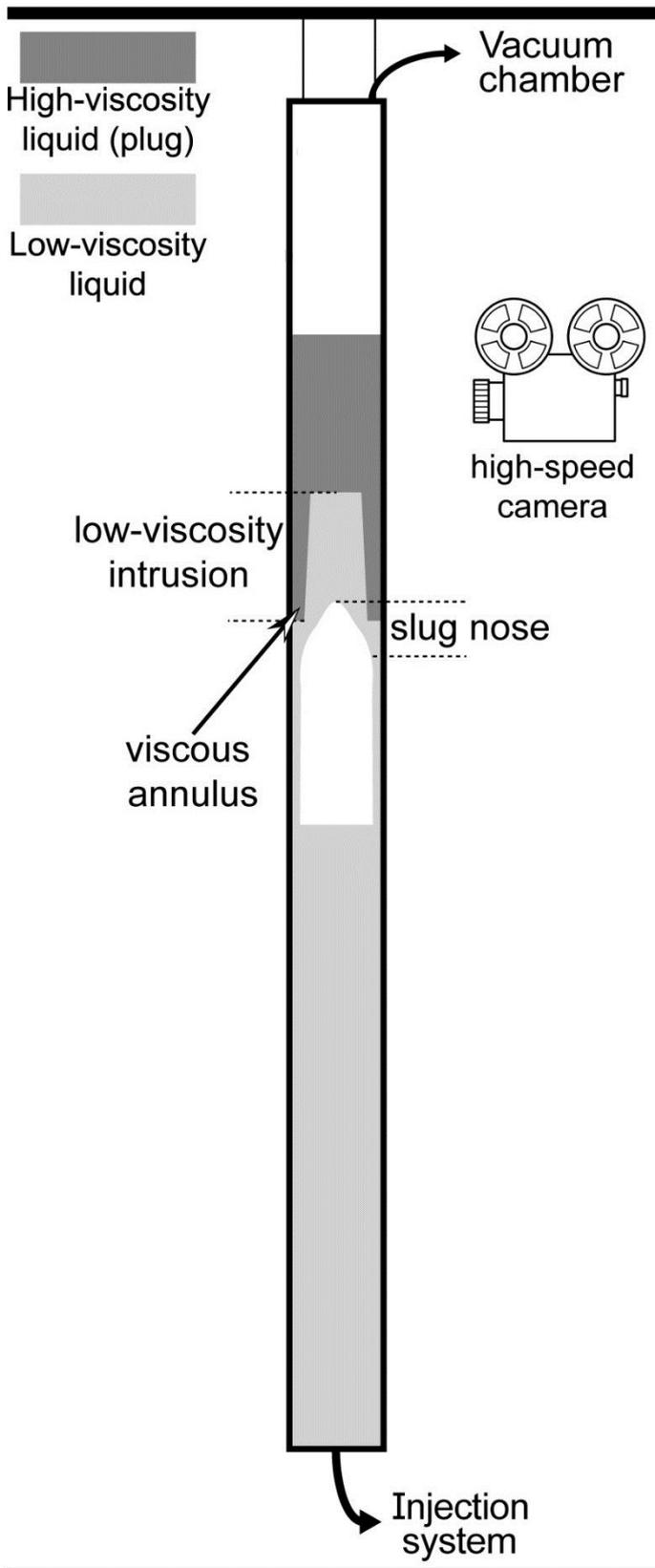
643 ^c calculated from equation (28) in Del Bello et al. (2012)

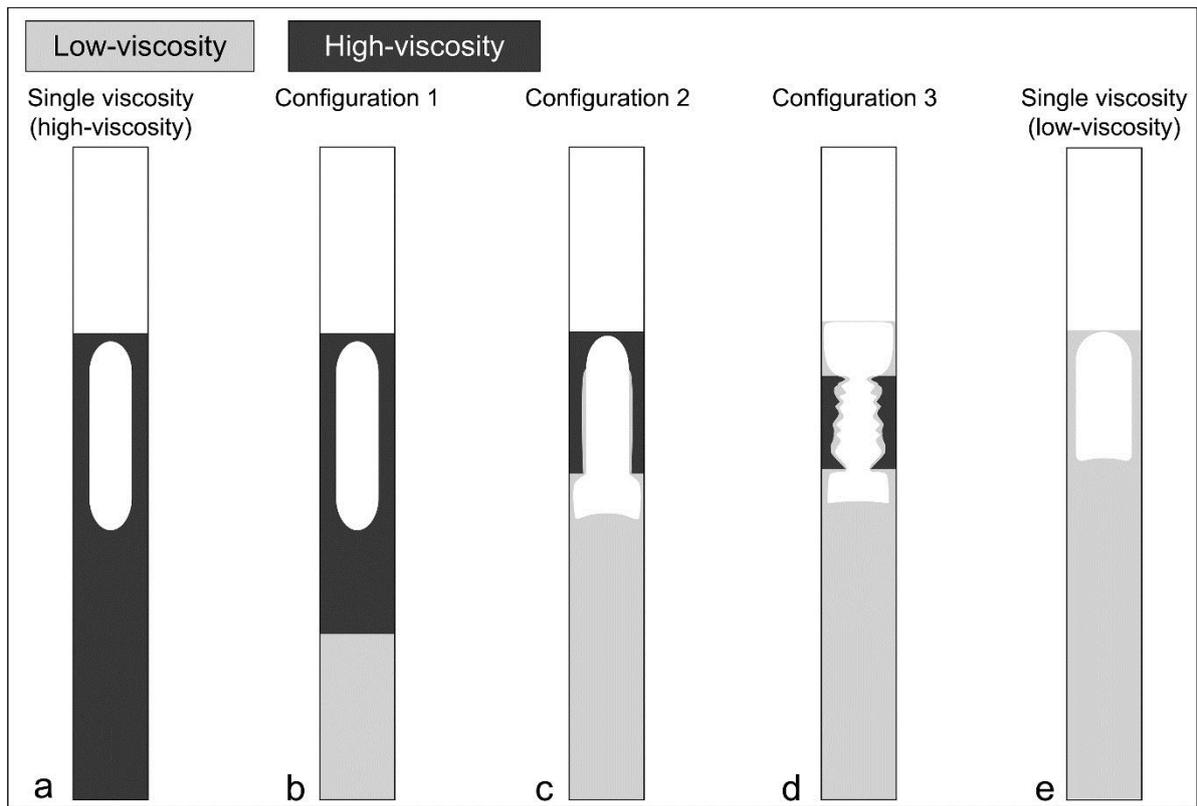
644 ^d calculated from equation (4.2) in Llewellyn et al. (2011)

645 ^e viscosity and density data reported in Gurioli et al. (2014)

646

geometrical parameters	
P_a	ambient pressure
P_0	initial bubble pressure
P	bubble pressure
L_0	initial bubble length
L	bubble length
h'_1	initial height of low-viscosity liquid above the slug
h'_3	initial height of the plug
h_1	height of low-viscosity liquid above the bubble
h_2	height of low-viscosity intrusion
h_3	depth from the plug top to the intrusion
$v_s t$	depth from the bubble base to the tube base
r_c	tube radius
r_s	bubble radius
r_p	viscous annulus radius
r_ϕ	intrusion radius
μ_1	viscosity of the liquid beneath the plug
μ_2	plug viscosity
ρ_1	low-viscosity liquid density
ρ_2	plug density

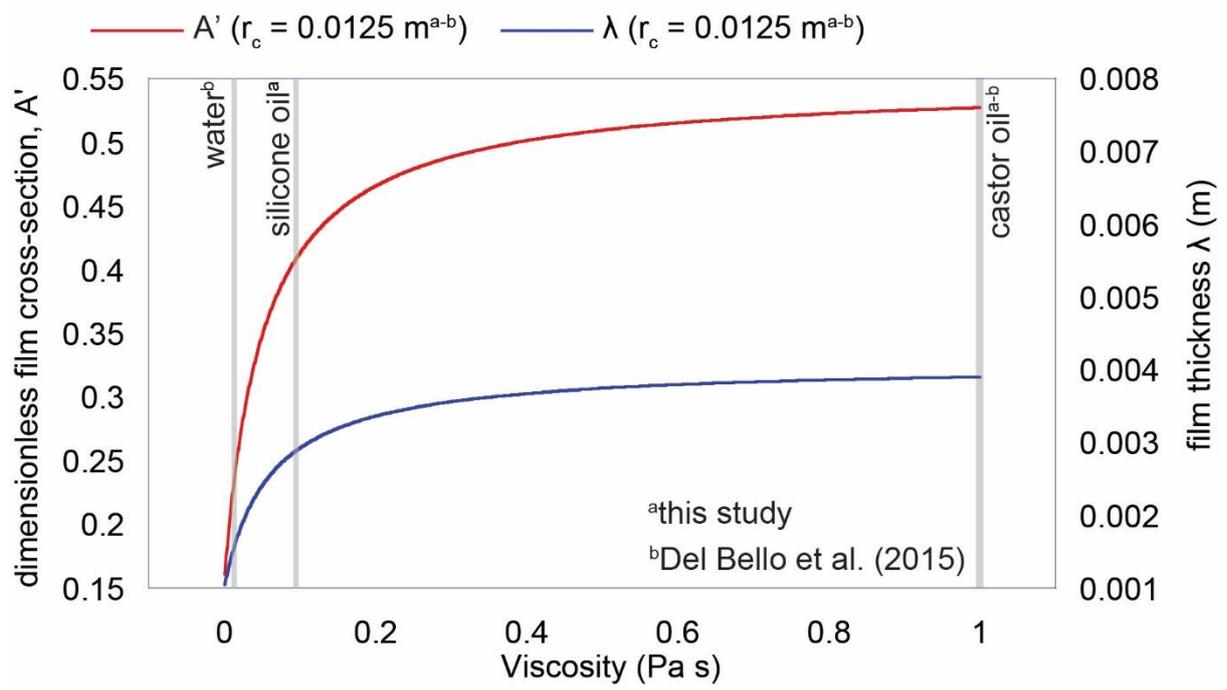




653

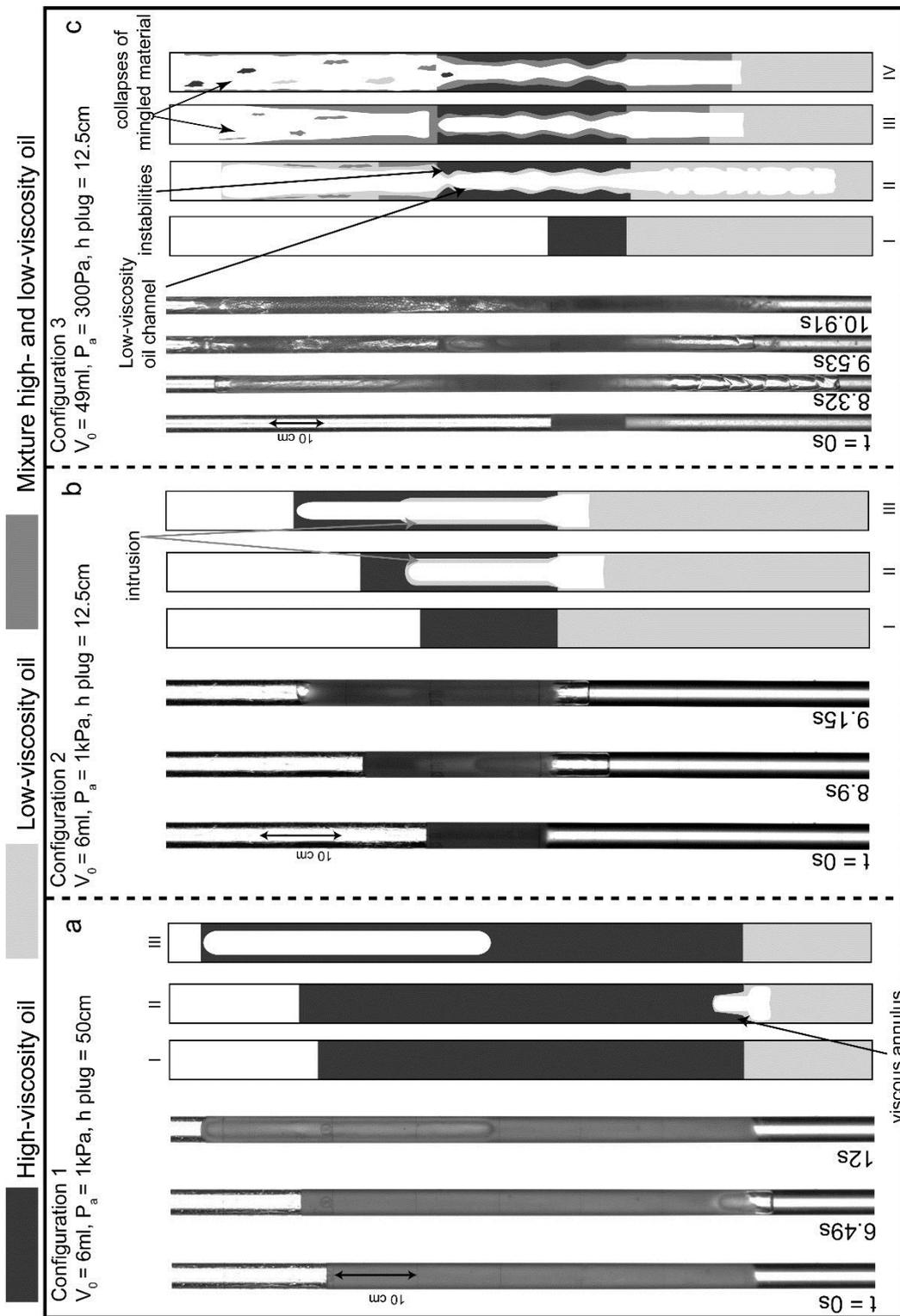
654

655 Figure 3

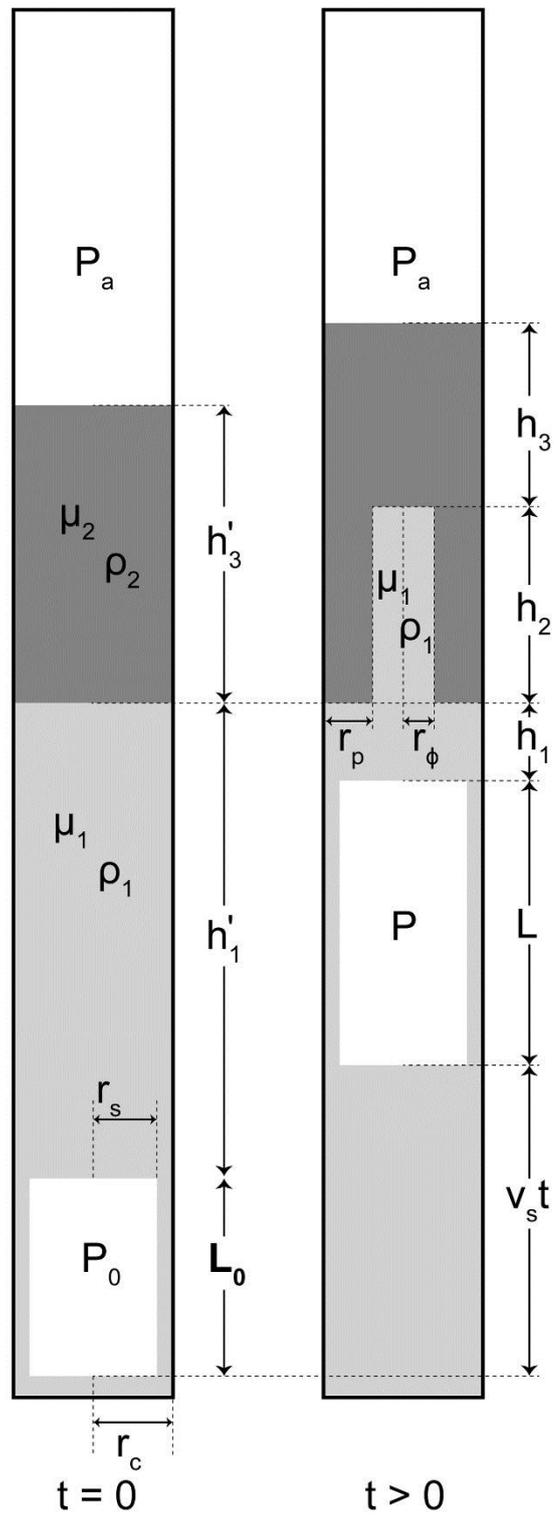


656

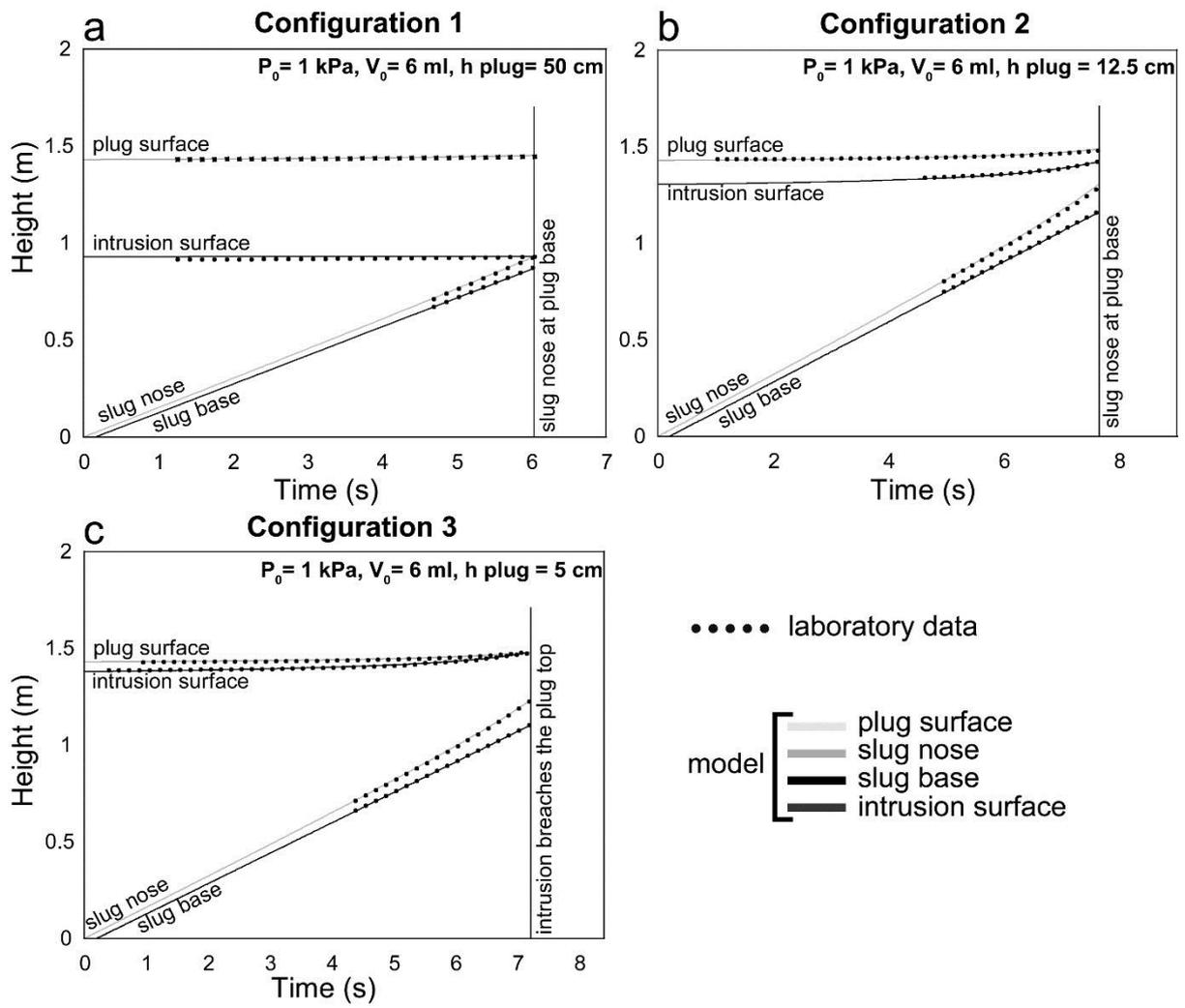
657



 High-viscosity liquid (plug)
 Low-viscosity liquid

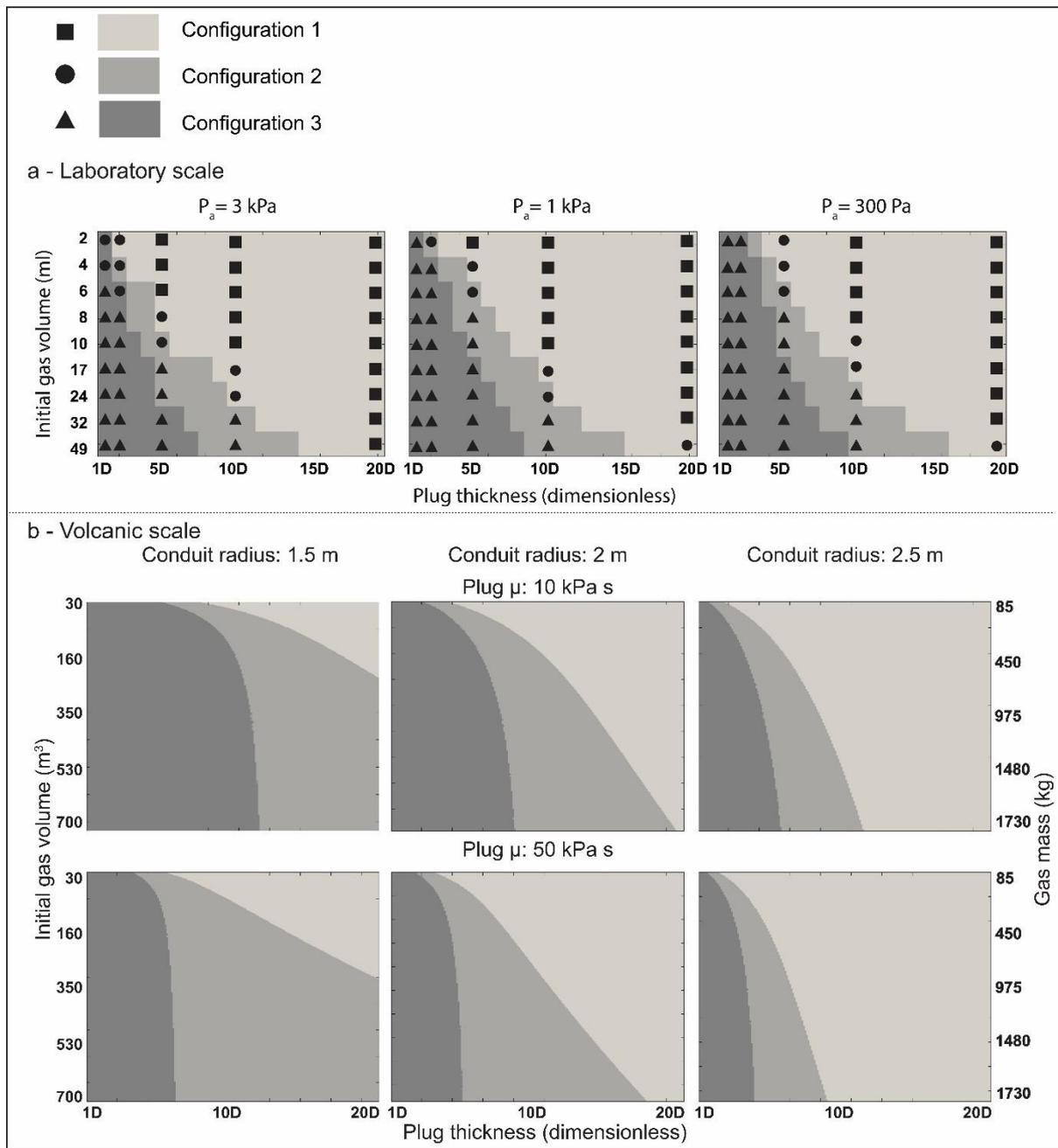


664 Figure 6



665

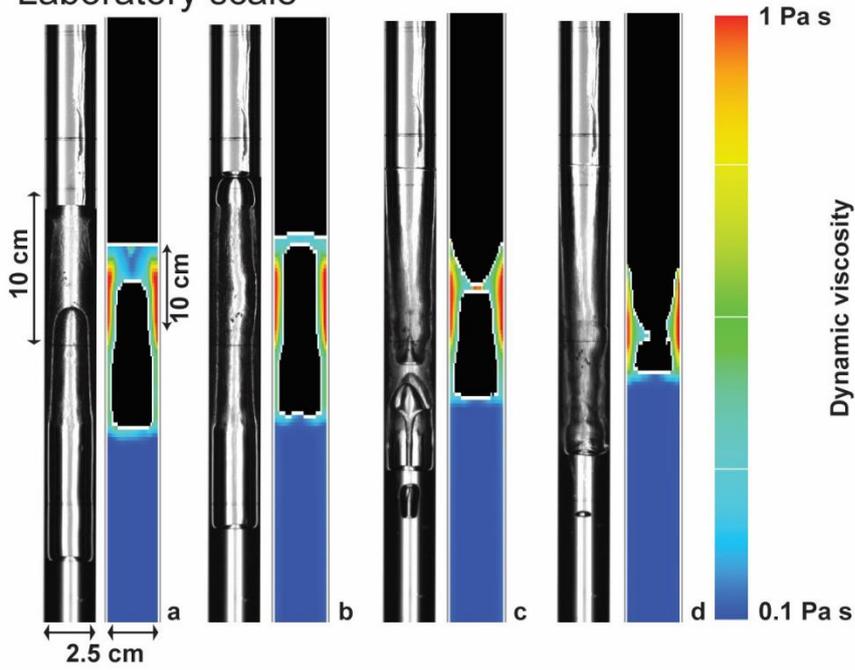
666



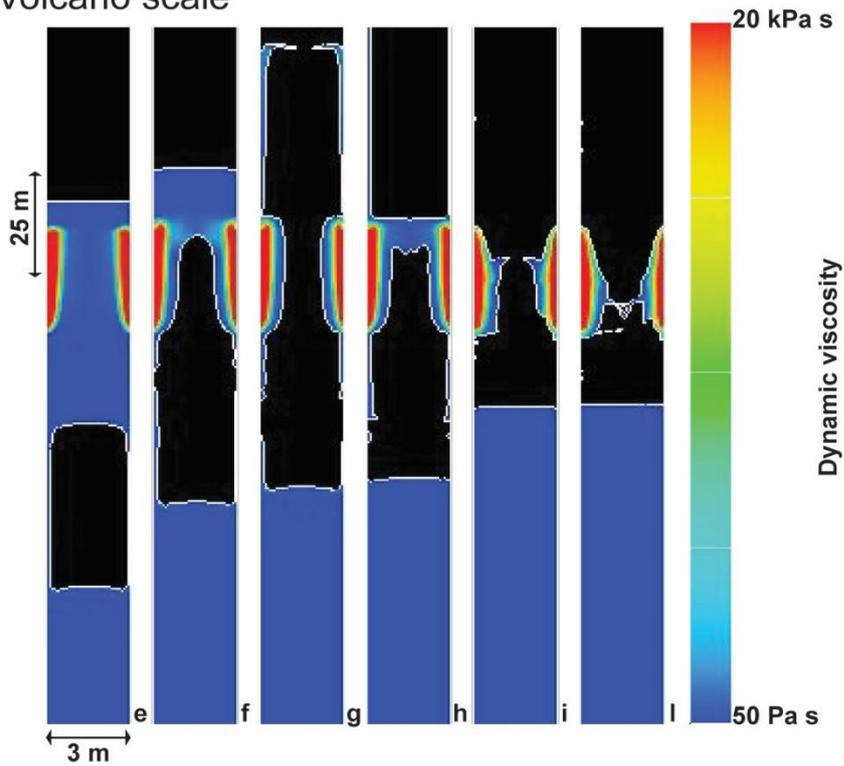
668

669

Laboratory scale



Volcano scale



673 **Figure Captions**

674 **Figure 1.** The experimental apparatus comprised a 3-m-high vertical tube, with a diameter D
675 of 0.025 m, connected to a vacuum chamber and a gas injection system. Scaling
676 considerations dictated that experimental ambient pressure was varied between 3 kPa, 1 kPa
677 and 300 Pa. Slug ascent, expansion and burst through the experimental liquids were imaged
678 with a high-speed camera at 300 fps. As a slug ascended and expanded in the tube, it drove an
679 intrusion of the underlying low-viscosity liquid into the plug, forming a low-viscosity
680 channel (**low-viscosity intrusion**). The intrusion displaced and spread the high-viscosity
681 liquid along the tube wall, creating a high-viscosity annulus (**viscous annulus**) that, in turn,
682 enclosed the intrusion.

683 **Figure 2.** Experimentally informed conceptual sketches of tubes filled with (a) high-viscosity
684 and (e) low-viscosity liquid represent the configuration end-members that sandwiched three
685 main flow configurations for the two-layer system. (b) Configuration 1: the viscous plug
686 volume fully accommodates the gas slug. (c) Configuration 2: the plug volume cannot
687 accommodate both the low-viscosity intrusion and the slug. At burst, the slug nose and main
688 body are in the plug, whilst the base is still in the low-viscosity liquid. (d) Configuration 3:
689 slug expansion drives the intrusion of low-viscosity liquid through the plug, extruding a low-
690 viscosity layer above the plug in which the slug burst. Instabilities develop as the slug passes
691 through the annulus into the extruded low-viscosity layer.

692 **Figure 3.** Variations of the dimensionless film cross section A' (calculated from equation
693 (28) in Del Bello et al. 2012) and thickness of the falling liquid film (m), λ , as function of
694 viscosity for a tube radius of 0.0125 m; shaded areas highlight the values for water ($\mu = 0.001$
695 Pa s, $\rho = 1000 \text{ kg/m}^3$; used in Del Bello et al. 2015), silicone oil ($\mu = 0.1 \text{ Pa s}$, $\rho = 990 \text{ kg/m}^3$;

696 this study) and castor oil ($\mu = 1 \text{ Pa s}$, $\rho = 961 \text{ kg/m}^3$; both this study and Del Bello et al.
697 2015).

698 **Figure 4.** Still frames and interpretative sketches from selected experiments representative of
699 the identified flow configurations are shown. (a) Configuration 1: as the slug rose, gas
700 expansion drove the intrusion of low-viscosity liquid into the plug (6.49 s); once the
701 transition between the liquids was complete, the slug was fully accommodated within the
702 plug (12 s). (b) Configuration 2: the slug exploited the low-viscosity intrusion, enclosed
703 within the viscous annulus, to ascend through the plug (8.9 s). This tri-axial flow comprises
704 ascending gas, descending low-viscosity liquid and, at flow timescale, relatively stationary
705 high-viscosity liquid. At burst: (i) the slug nose was within the viscous plug, (ii) the low-
706 viscosity film and the viscous annulus surrounded the slug main body (tri-axial flow), and
707 (iii) the slug base remained in the low-viscosity liquid below the plug (annulus) base (9.15 s).
708 (c) Configuration 3: the low-viscosity intrusion breached the plug top, and the slug burst into
709 the extruded low-viscosity layer (8.32 s); instabilities formed and propagated along the
710 falling film, leading to bubble break-up, partial blockage of the conduit and mixing between
711 liquids (9.53 s). At burst, globules of this mixture fell back on the liquid surface (10.91 s).

712 **Figure 5.** The 1D model geometry for a gas slug ascending in a low-viscosity liquid overlaid
713 by a high-viscosity liquid is shown. White regions represent the gas bubble, while grey-scale
714 regions the liquids. See Table 2 for a complete geometrical notation.

715 **Figure 6.** Comparison of slug ascent profiles measured from laboratory video (symbols) and
716 the 1D model (lines) for each flow configuration. A 6 ml slug ascends in a liquid column
717 overlain by a plug of 50 cm (Configuration 1; a), 12.5 cm (Configuration 2; b) and 5 cm
718 (Configuration 3; c) with a $P_a = 1 \text{ kPa}$. In all cases the variations in position of the plug
719 surface, intrusion surface, slug nose and slug base are well reproduced. For Configuration 3

720 (c), the intersection between the plug and intrusion curves indicates that the low-viscosity
721 liquid breached the plug surface. The comparison with the experimental data is limited up to
722 the moment the simulation stopped. Note that video data for the slug ascent are not available
723 for heights $< \sim 0.5$ above the apparatus base, because of the camera field of view.

724 **Figure 7. (a)** Comparison between experimental fluid configurations (symbols) and
725 configurations forecasted by the 1D model (shaded regions) is shown as a function of initial
726 gas volume (ml) and plug thickness (dimensionless), for ambient gas pressures of 3 kPa (left),
727 1 kPa (middle) and 300 Pa (right). **(b)** Flow configurations forecast by the 1D model for an
728 idealized volcanic scenario are shown, for a plug viscosity of 10 kPa s (upper row) and 50
729 kPa s (lower row), and as function of initial gas volume (m^3), or gas mass (kg; right axis),
730 plug thickness (dimensionless) and volcanic conduit radii of 1.5 (left), 2 (middle) and 2.5
731 (right) m; the configuration distribution is insensitive to the viscosity of magma beneath the
732 plug within the limit 50-500 Pa s.

733 **Figure 8. (upper panel)** Still frames from a laboratory experiment and 3D CFD simulation
734 for a 10 ml slug, expanding in a $P_a = 3$ kPa and a plug $h = 12.5$ cm (Configuration 3). The
735 CFD simulation reproduced experimental observation well, including the variations in slug
736 shape, intrusion dynamics, burst dynamics and bubble breakup process (see also Video V05).
737 Note the asymmetry in panels **c** and **d** that demonstrate the requirement for full 3D
738 simulation. **(lower panel)** Still frames from a 3D CFD simulation at volcanic-scale. Input
739 parameters are $V_0 = 140 \text{ m}^3$, $P_a = 10^5 \text{ Pa}$, $\mu_{\text{magma}} = 50 \text{ Pa s}$, $\mu_{\text{plug}} = 20 \text{ kPa s}$, $r_c = 1.5 \text{ m}$, column
740 $h = 200 \text{ m}$, conduit radius $r_c = 1.5 \text{ m}$, conduit $h = 300 \text{ m}$, and plug $h = 15 \text{ m}$. Note the visible
741 asymmetry that develops once instabilities arise from panel **g** onward, underscoring the
742 requirement for a 3D approach once dynamic instability develops.