



Optimisation of tower site locations for camera-based wildfire detection systems

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A tower site selection optimisation framework which may be used to configure camera-based wildfire detection systems in vast, complex terrains is presented. The framework can obtain multiple practical layouts within days, allowing more rapid planning, deployment and activation of new systems compared to what has been possible with conventional methods.

For Review Only

Optimisation of tower site locations for camera-based wildfire detection systems

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Abstract

Early forest fire detection can effectively be achieved by systems of specialised tower-mounted cameras. With the aim of maximising system visibility of smoke above a prescribed region, the process of selecting multiple tower sites from a large number of potential site locations is a complex combinatorial optimisation problem. Historically, these systems have been planned by foresters and locals with intimate knowledge of the terrain rather than by computational optimisation tools. When entering vast new territories, however, such knowledge and expertise may not be available to system planners. A tower site-selection optimisation framework which may be used in such circumstances is described in this paper. Metaheuristics are used to determine candidate site layouts for an area in the Nelspruit region in South Africa currently monitored by the ForestWatch detection system. Visibility cover superior to that of the existing system in the region is achieved and are obtained in a number of days, while traditional approaches normally require months of speculation and planning. Following the results presented here, the optimisation framework is earmarked for use in future ForestWatch system planning.

Keywords: Fire detection, maximal cover, optimisation, facility location, NSGA-II

1 Background

Wildfires, when left untreated and under the right conditions, can spread rapidly and go on to cause enormous destruction to rural and urban landscapes. The early detection of their onset is of critical importance – the sooner suppressing action can be taken, the more manageable the size of the fire may be, potentially allowing minimisation of the scale of destruction (Rego and Catry, 2006). Camera-based wildfire detection systems (CWDSs) provide early detection in the form of a number of specialised cameras that monitor the surrounding environment (Martell, 2015). The research presented here has been conducted in collaboration with EnviroVision Solutions, which operates the South African-developed ForestWatch CWDS in South Africa, Australia, Spain, Canada and the USA.¹ ForestWatch CWDSs monitor the surrounding environment for smoke using a proprietary pattern-recognition algorithm which is based upon South African Antarctic research into the automated detection of aurora (Hough, 2007). Once smoke is detected, human operators at dedicated workstations – located at detection centres of local fire protection agencies – are alerted in order to validate fires and send out detection reports. The location of a fire is estimated by

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¹The corresponding author is not affiliated with EnviroVision Solutions, but has served as a volunteer fire fighter during multiple wildfires in the South African Western Cape and has a keen interest in fire detection and prevention.



Figure 1: (a) Camera used in ForestWatch fire detection systems; (b) a 32-m tower on top of which a camera is placed, with the solar power supply visible near the base of the tower.

14 triangulation if the smoke is visible from two or more cameras, or from the location of the smoke within an
 15 image when only visible from one camera (Matthews et al., 2012).

16 Figure 1(a) shows a typical camera, while a 32-m tower with a camera mounted on top is displayed
 17 in Figure 1(b). Terrain features and vegetation growth cause varying degrees of obstruction between the
 18 cameras in a CWDS and possible smoke plumes, as seen in Figure 2. The towers are therefore typically
 19 placed at elevated sites which have good visibility of their surroundings, *e.g.* peaks on mountains and hills.
 20 Cost considerations mean that potential sites that offer good visibility will generally far outnumber the
 21 camera towers available for placement. The challenge is therefore to identify at which sites to place the
 22 towers. This is an intricate process, since the overall system detection potential relies on more than simply
 23 identifying a number of sites according to their individual visibility cover, but rather the identification of a
 24 combination of sites that offer the best *combined* system visibility cover.

25 Literature on the topic of candidate site identification intended for CWDS purposes is scarce – two recent
 26 publications, however, demonstrate typical approaches that may be followed. Bao et al. (2015) followed an
 27 approach in which thirty candidate sites were manually identified from peaks and ridges on hilltops within
 28 a relatively small study area of 10 km². Candidate layouts were then determined from the thirty sites
 29 for CWDSs comprising between six and sixteen towers, using integer programming (Newman and Weiss,
 30 2013) and a genetic algorithm similar to the one employed later in this paper. The manual site selection
 31 approach followed by Bao et al. (2015) is not considered desirable here, as it would be impractically laborious
 32 and time-consuming for the intended application considered here. The average ForestWatch system covers
 33 surface areas of well over 1 000 km² which contain numerous mountains, hills and ridges that may be
 34 considered for tower placement – significantly larger and more complex than the area considered by Bao
 35 et al. (2015). The manual candidate site identification and evaluation process took over five months for
 36 the existing ForestWatch system considered below which monitors an area of 1 505 km². Shortening the
 37 duration of such processes to allow wildfire detection systems to become active earlier is a driving factor
 38 behind ForestWatch's interest in optimisation methods.

39 The second candidate site identification approach was proposed by Eugenio et al. (2016) using Geo-
 40 graphical Information Systems (GIS) software, when they selected sites for manned watchtowers in an area



Figure 2: Fires detected by the ForestWatch CWDS, displaying typical visibility obstruction that may be caused by (a) terrain, and (b) vegetation.

41 covering 46 000 km². GIS processes were used to identify land within feasible geographical and adminis-
 42 trative/municipal boundaries, while terrain feature classification analyses were used to identify ridges on
 43 mountains and hills. Areas on the terrain that were within suitable distances of roads were also identified.
 44 The area that satisfied all three criteria of feasible land, ridge features, and suitable road access areas resulted
 45 in a final feasible terrain surface which was considered for watchtower placement. The study area was then
 46 sub-divided into uniform square cells of 15 × 15 km and the feasible site with the highest altitude in each
 47 cell was specified as a watchtower site. This method of site identification offers a relatively simple method
 48 of identifying multiple sites across a very large surface area. The disadvantage of such an approach is that
 49 the sites are identified according to the expected visibility of each individual watchtower, based upon terrain
 50 features and altitude. This may yield good individual tower visibility, but neither considers nor guarantees
 51 good overall system cover (Franklin and Clark, 1994; Rana, 2003; Kim et al., 2004).

52 The standard approach in similar surveillance/detection research is to evaluate a system's detection
 53 potential with respect to the terrain surface only (Franklin, 2002; Kim et al., 2004; Bao et al., 2015).
 54 However, ForestWatch systems detect smoke patterns *above* the terrain surface (Schroeder, 2005; Hough,
 55 2007), and as the smoke rises, it typically needs to clear interference from terrain and vegetation to be
 56 detectable as shown in Figure 2. The lower above the terrain surface a smoke plume may be detected, the
 57 sooner an alert may be generated and suppressing action initiated. A CWDS's potential for detecting smoke
 58 at *multiple* levels above the terrain surface therefore plays a role in gauging its effectiveness for near-surface
 59 (early) and higher (secondary) smoke detection. CWDSs may also be configured with consideration given
 60 to their visibility cover achieved over buffer zones which extend coverage beyond the client boundaries. This
 61 is because external fires may well encroach onto the client area, meaning that external fires are also crucial
 62 to monitor. Two smoke detection heights and a buffer zone are considered in the evaluation of candidate
 63 system layouts here, resulting in a coverage maximisation problem with two objectives. ForestWatch have
 64 also expressed their intention to incorporate additional objectives in future work, including the maximisation
 65 of backup (overlapping) cover (Hogan and Revelle, 1986; Heyns and van Vuuren, 2016), the maximisation
 66 of their towers' triangulation accuracy in determining fire locations, and cost minimisation. As a result,
 67 the process of configuring CWDS layouts becomes a complex Multi-Objective combinatorial optimisation
 68 problem, for which recent novel approaches are necessary (Heyns, 2016).

69 The first steps taken towards a comprehensive CWDS tower-site selection optimisation framework are
 70 presented. The main aim was to provide an approach capable of determining multiple, high-quality CWDS
 71 layouts within practical computation times. Multiple candidate layouts allow decision makers to evaluate the
 72 trade-offs between different layouts when selecting a final solution. An area in the Nelspruit region in South
 73 Africa, which is currently covered by an existing ForestWatch CWDS, was used as the study area, and the
 74 optimisation framework was used to compute CWDS layouts comprising twenty cameras. A Multi-Objective
 75 Evolutionary Algorithm (Cheshmehgaz et al., 2015) combined with a multi-resolution approach (Heyns and

76 van Vuuren, 2016) is proposed for the optimisation of CWDS layouts. This algorithm considers areas that
77 are deemed feasible for tower placement, which are determined by terrain characteristics and proximity to
78 features such as roads. The quality of the generated CWDS layouts is determined by evaluating the coverage
79 of two smoke layer heights over primary and buffer zones. The outputs included multiple candidate CWDS
80 configurations and visibility coverage maps which may be analysed by decision makers before a final layout
81 is selected.

82 **Methods**

83 *Study area and existing tower sites*

84 In order to demonstrate the practicality and effectiveness of this research for future tower site-selection
85 problems, a comparative platform had to be established for evaluation purposes. An existing CWDS of
86 twenty six cameras was identified by ForestWatch experts for this purpose. This CWDS is located in the
87 vicinity of Nelspruit, in the north-east of South Africa, and monitors forestry plantations. This specific
88 system was selected because of its mountainous and challenging terrain (see Figure 2) and because the
89 existing CWDS is reliable and regularly detects potential fires on a daily basis. In 2017 alone, the system
90 logged 2786 alerts within the subscribed client area, and many more outside.² Wildfires in the region
91 occur primarily between July and October (Strydom and Savage, 2016), with the most recent large wildfire
92 occurring in August 2016 and destroying over 2 500 hectares of plantations and natural forests. An additional
93 reason for the selection of this CWDS as a basis for comparison was that experts with extensive experience
94 in the region were available for feedback and discussions.

95 The client area is non-contiguous and covers a surface area of approximately 1 505 km². The cameras have
96 a specified detection range of 8 km and are placed on towers that range in height from 12 m to 54 m at the
97 locations shown in Figure 3.³ The planning of the existing CWDS layout was a collaborative effort between
98 ForestWatch technicians, GIS managers from the forestry clients, and local experts. Numerous potential
99 sites were manually identified over five months in 2010, and this was followed by physical inspections to
100 assess the sites according to their distance from power lines, access to roads, and site security (vandalism
101 and theft are common in the region). Six of the sites were easier to select than the others and are indicated
102 as “preferred sites” in Figure 3. These are the sites of old watchtowers and were selected without need for
103 deliberation because of the existing infrastructure, road access and historically proven visibility cover. The
104 remaining twenty sites required further investigation, analysis and comparison with other sites in terms of
105 the aforementioned criteria and predicted coverage potential.

106 The base tower structure height that was used by ForestWatch for this system is 12 m. However,
107 extensions to base tower heights are often added because an increase in tower height improves overall smoke
108 detection potential by allowing a camera to see over obstructions. When required, height increases were
109 achieved by adding extensions to the base structure, generally in increments of 3 m. The requirement for an
110 increase in tower height at each site depended on a) whether surrounding vegetation demanded an increase
111 in tower height so that the camera could rise above the trees’ canopy, b) the actual need for an increase
112 in tower height, depending on client coverage already achieved from the base tower height, and c) whether
113 the terrain could accommodate the demands of an increase in structure size and support (in terms of the
114 tower foundation and stabilisation wires that increase in span as tower height increases). The criterion of
115 proximity to power supplies was eventually dismissed, and solar power supplies were installed at all sites
116 due to an inconsistent power supply system in the region (a solar power supply can be seen in Figure 1(b)).

117 *Terrain modelling and viewshed analyses*

118 Raster data represent the earth’s surface and geospatial information as uniformly spaced sample points
119 across the terrain and are used for both the terrain model and candidate site selection in this paper. Raster

²While many of these fires are authorised prescribed burns or smoke rising from informal settlements on the edges of the client area, fires that are actual threats are also regularly detected.

³The actual detection range of the cameras is well over 8 km, and fires are often detected at twice this range. The range of 8 km is used for contractual purposes and to mitigate the negative effects of bad weather on practical detection potential.

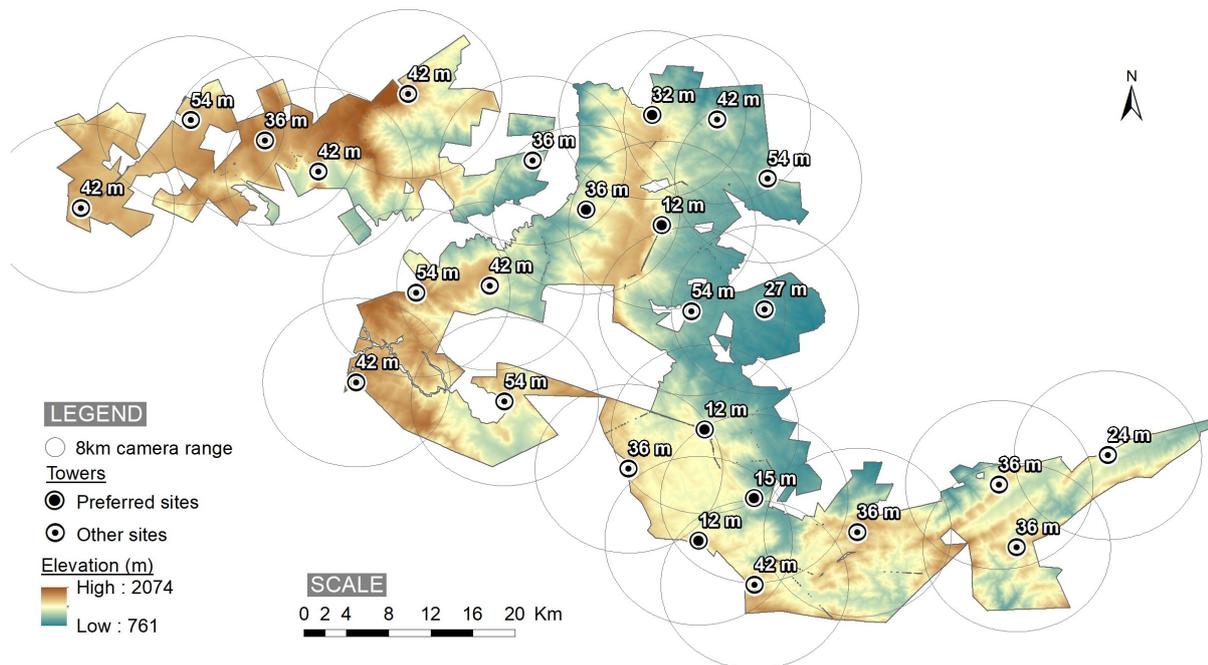


Figure 3: Top view in relief of the ForestWatch system and client area that was identified to provide a benchmark for the evaluation of the optimisation approach followed in this paper.

120 data are employed extensively for solving facility location problems due to their simplicity and ease of
 121 implementation (Franklin, 2002; Kim et al., 2004; Tanergüçlü et al., 2010; Kwong et al., 2014; Heyns and
 122 Van Vuuren, 2015).

123 An example of a raster data representation of terrain is provided in Figure 4(a). The non-contiguous
 124 blue area in the figure is an example of terrain that has been identified as suitable for the placement of
 125 towers after the identification of feasible placement regions. The green area is an example of an area of
 126 interest, which in this paper, is typically land belonging to one or more forestry clients. The terrain surface
 127 in this figure is, in fact, generated from sampled (raster) elevation data with the dots being on the terrain
 128 surface. The distance between neighbouring sample points is approximately 30 m at the highest resolution
 129 of raster data that is typically available to the public. The sites within the area that may be considered for
 130 facility placement (the blue dots) collectively form what is referred to as the Placement Zone.

131 The CWDS's detection potential is determined with respect to smoke above the terrain surface that
 132 falls within the client and buffer boundaries. As mentioned above, this process is performed with respect to
 133 multiple smoke heights, and each specified smoke detection height can be depicted as a smoke layer following
 134 the contour of the terrain. The smoke layers and their associated boundaries are termed Cover Zones, *i.e.*
 135 areas with respect to which a CWDS's visibility cover is determined. As is the case for the Placement Zone,
 136 Cover Zones are represented by raster data and are the rasterised terrain surface that falls within client
 137 and buffer boundaries raised to specified heights, as illustrated in Figure 4(b) for a Cover Zone (the brown
 138 surface and markers) above the client area.

139 The portion of a Cover Zone that is visible from a camera is referred to as a *viewshed*, and is computed
 140 from a collection of line-of-sight queries calculated between the camera and all the demand points within the
 141 Cover Zone, limited by terrain interference and the camera's detection range (Nagy, 1994; Franklin, 2002;
 142 Kim et al., 2004). A CWDS's viewshed of a Cover Zone is then the merged viewsheds of all the individual
 143 cameras in the system with respect to the Cover Zone – *i.e.* the demand points in the Cover Zone that are
 144 visible from at least one camera in the system. Figure 4(c) provides a top view of the terrain discussed in
 145 Figures 4(a) and (b), and an example of a CWDS viewshed (the red surface and markers) achieved by an

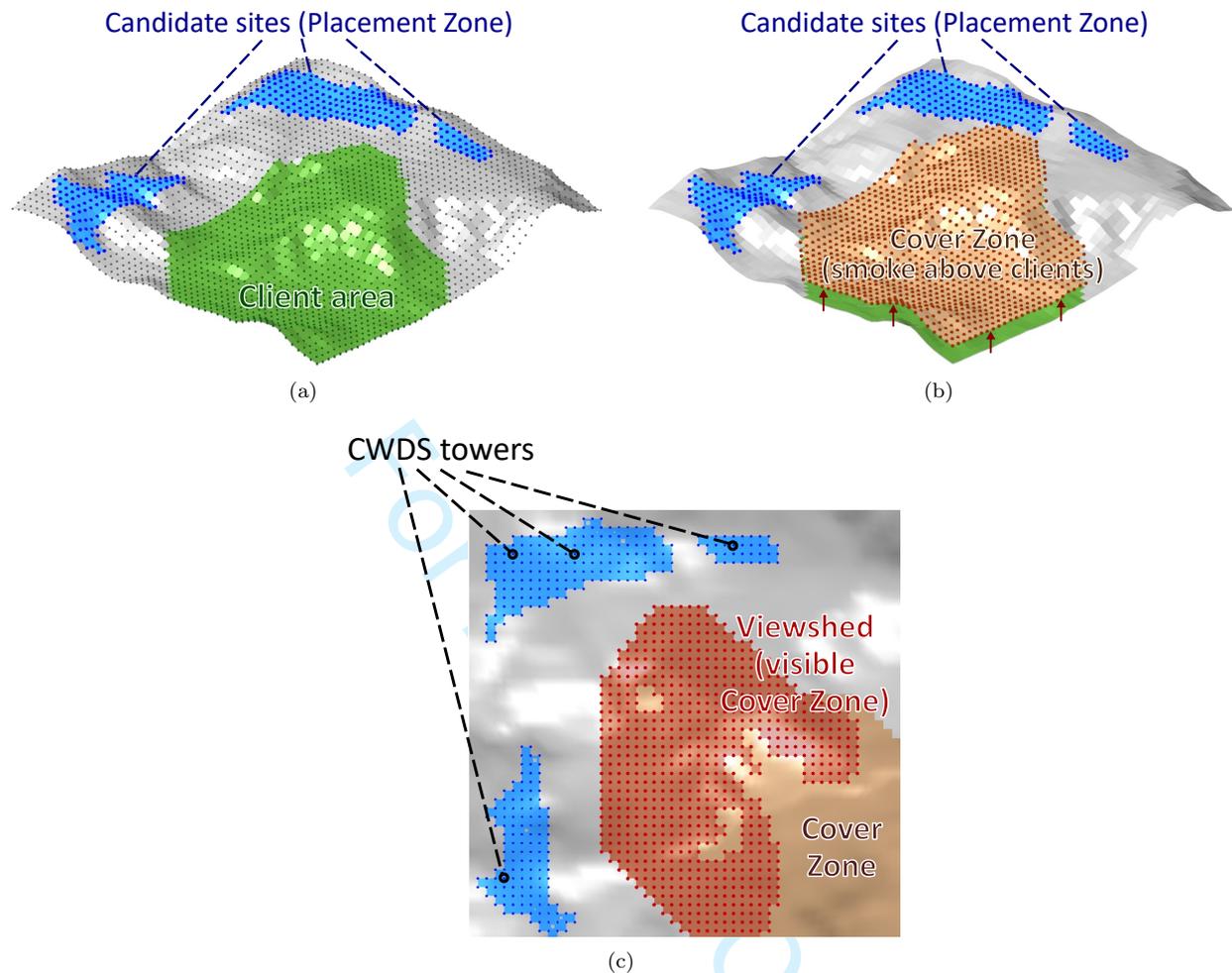


Figure 4: Raster data represent the earth's surface as uniformly spaced sample points. (a) Raster representation of a terrain surface with a Placement Zone and client area; (b) raster representation of a Cover Zone above the client area; (c) top view of the terrain, displaying an example CWDS tower layout (the black markers) and its viewshed achieved with respect to the Cover Zone (the red area and markers).

146 example tower site layout for a system with four cameras (the black markers).

147 *Placement Zone specification*

148 The basic criterion to consider in the process of identifying a feasible Placement Zone is that towers may
 149 only be placed at sites within the client area because properties outside this area belong to entities that do
 150 not collaborate with ForestWatch. Two additional geospatial criteria were identified by ForestWatch experts
 151 as vital in determining site suitability. First, only terrain with a degree of slope under 12° (or 20%) should
 152 be considered to ensure that tower installation may be performed without the need for excessive terrain
 153 alteration, in addition to ease of access on foot. Second, a distance of 100 m or less to roads is deemed
 154 necessary for transportation (*e.g.* construction and maintenance) and general access purposes. Selecting the
 155 candidate sites according to criteria such as altitude and terrain features, as proposed by Eugenio et al.
 156 (2016), would reduce the number of sites in the Placement Zone. However, there is a risk that high-quality
 157 candidate sites may be discarded by this approach, so it was not considered further.

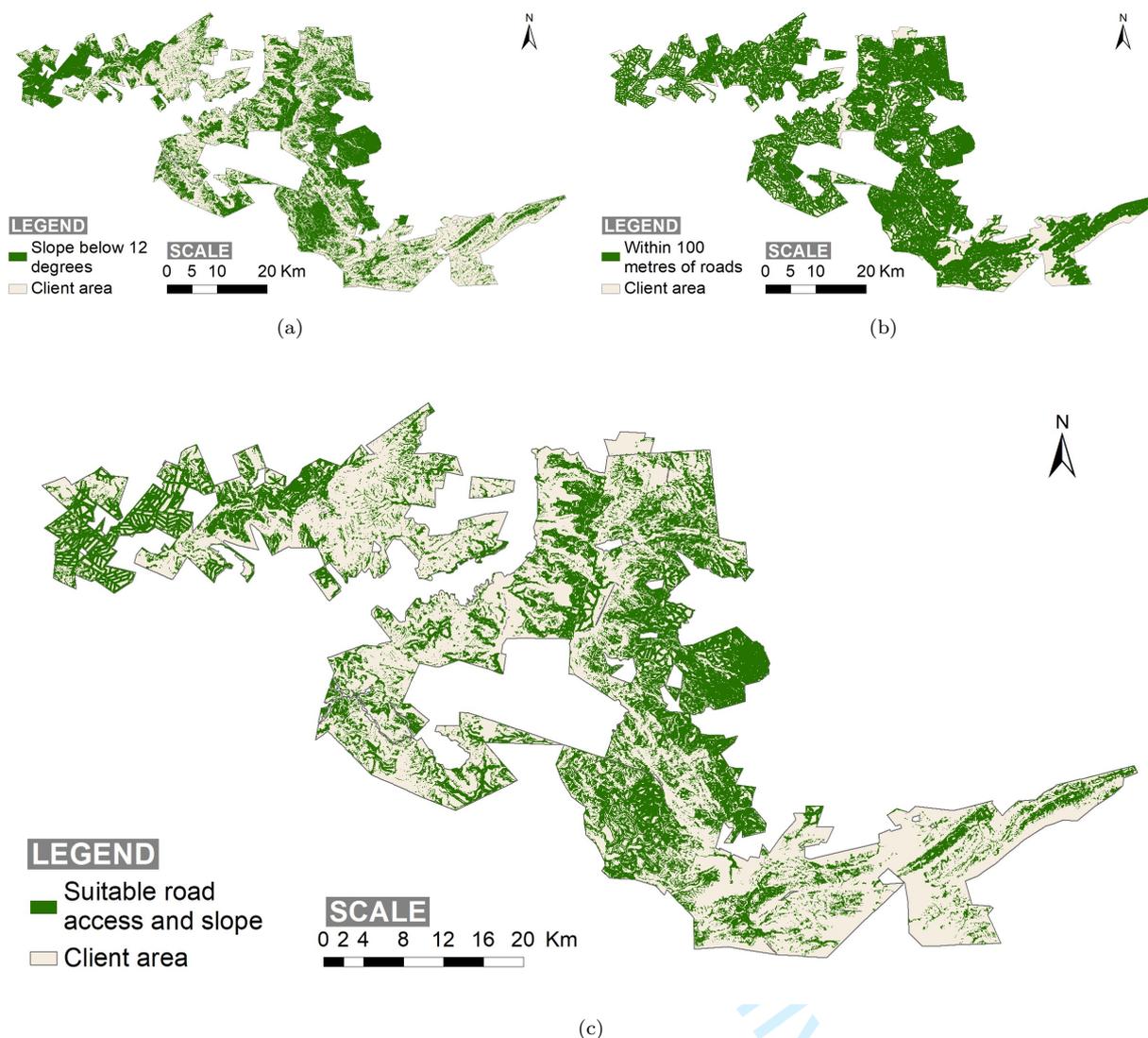


Figure 5: Determination of the feasible Placement Zone within the client area. (a) Terrain degree of slope under 12°; (b) within 100 m of roads; (c) Placement Zone, where both slope and road access are feasible.

158 The commercially available ArcGIS 10.5.1 software⁴ was used to process the data required to determine
 159 suitable sites according to slope and road access. Feasible slope sites were determined with 30 m resolution
 160 raster elevation data and the ArcGIS slope tool, while road-accessible sites were determined with roads data
 161 obtained from the clients in the study area and the ArcGIS Euclidean distance analysis tool. The feasible
 162 slope and road access areas are displayed in Figures 5(a) and (b), respectively, and Figure 5(c) shows the
 163 resulting Placement Zone where both slope and road access are feasible. The number of candidate sites
 164 from the raster representation of the Placement Zone totals 741 813. The locations of the 26 towers of the
 165 existing system are all placed at sites in the feasible Placement Zone, indicating that the feasibility criteria
 166 considered here are indeed realistic.

⁴Developed by Environmental Systems Research Institute (ESRI), www.esri.com.

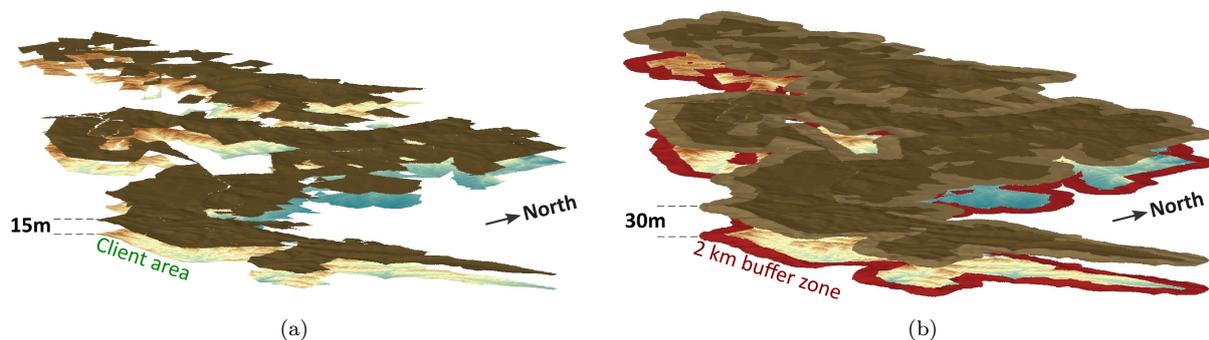


Figure 6: Client area and smoke layers viewed in perspective from the south-east, showing (a) 15-m and (b) 30-m smoke layers above the client area with a 2-km buffer zone being included in (b).

167 *System evaluation*

168 Two smoke layer heights were agreed upon for the evaluation of the benchmark and optimisation systems:
 169 15 m and 30 m.⁵ An illustration of the client area viewed in perspective from the south-east, with a 15-m
 170 smoke layer which follows the contours of the terrain, is provided in Figure 6(a). The smoke layer's actual
 171 height above the terrain surface is exaggerated for illustrative purposes. The purpose of the 15-m smoke
 172 layer is for near-immediate detection above the client area and is aimed at rapid response.

173 The 30-m smoke layer is shown in Figure 6(b) and includes a 2-km buffer zone which extends beyond the
 174 client area. The purpose of this smoke layer is for the detection of smoke that may not have been visible at
 175 15 m above the client area due to obstructions, and which has risen further to clear the obstructions to be
 176 (potentially) visible at 30 m. Furthermore, the buffer zone added to the smoke layer allows monitoring of
 177 the progress of fires outside the client area – fires which need to be monitored by ForestWatch, but which
 178 do not necessarily require client response if their properties are not under immediate threat.

179 It was made clear by ForestWatch experts that the towers placed at the six existing sites (indicated by
 180 full markers in Figure 3) were non-negotiable in the original site-selection process. It was decided to follow
 181 a similar approach during the optimisation process, so these six towers were considered as “existing” and
 182 included in all developed CWDSs by default. This approach mimics a scenario that is frequently encountered,
 183 where new towers are to be sited around existing towers to expand an existing system's coverage over new
 184 clients or blind spots, for example. The actual tower site selection process thus focused on selecting the sites
 185 for the remaining twenty towers.

186 The six existing towers and the coverage they achieve with respect to the smoke layers are shown in
 187 Figures 7(a) and (b). Since the indicated areas are already visible to these towers and are thus covered, the
 188 placement of additional towers does not require coverage of these areas. The remaining uncovered areas of
 189 the smoke layers, shown in Figures 7(c) and (d), are then the Cover Zones used to evaluate the coverage of
 190 the remaining 20 towers – Cover Zone 1 (15-m smoke height) and Cover Zone 2 (30-m smoke height with a
 191 2-km buffer). The aim of the study was therefore to use an optimisation approach to determine new CWDS
 192 layouts and to compare their coverage to that of the tower sites of the existing CWDS.

193 The optimisation process followed here focuses on initial, computational site selection and does not
 194 include the physical site inspection process where height added to that of the base tower height is considered.
 195 This means that only the base tower height of 12 m is considered during the optimisation process, and
 196 viewsheds are therefore determined from this observer height above the terrain surface. In order to provide
 197 a fair comparative platform, the benchmark cover achieved by the existing towers is determined at simulated
 198 tower heights of 12 m with respect to the Cover Zones. Under this assumption, the existing towers were
 199 determined as being able to see 56.0% of the demand points in Cover Zone 1 and 54.6% of those in Cover

⁵The heights chosen here are for the investigative purposes of this research. Future projects may well include more than two smoke layer heights and different heights to those considered here.

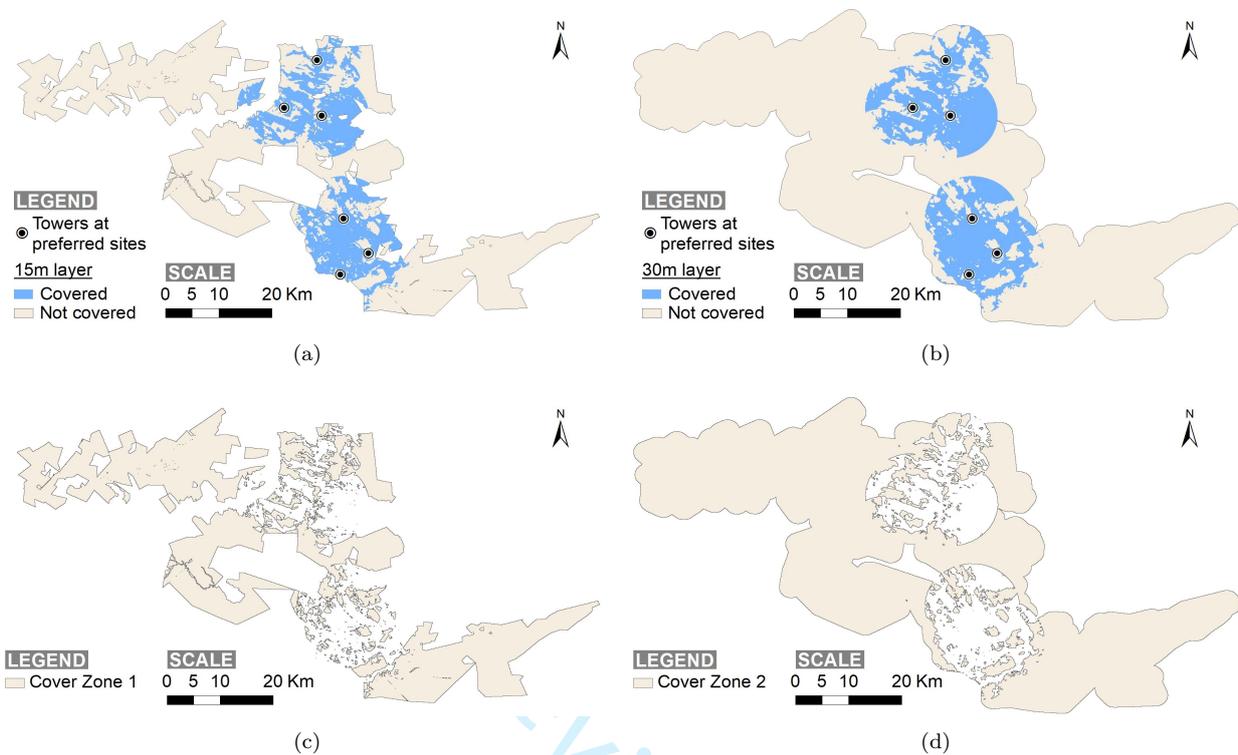


Figure 7: The process followed to determine the Cover Zones used for system evaluation in this paper. Cover achieved from six existing towers (determined at a detection range of 8 km and their actual heights) that are included in the optimisation approach are shown with respect to (a) a 15 m smoke layer, and (b) a 30 m smoke layer with a 2 km buffer. This cover is removed from the smoke layers and result in (c) Cover Zone 1, and (d) Cover Zone 2.

200 Zone 2, as shown in Figure 8 (the demand points in the Cover Zones are spaced at the same raster resolution
 201 as that of the Placement Zone, namely 30 m). For reference, the twenty towers at their actual heights (an
 202 average of 42 m) achieve 64.5% and 61.1% coverage with respect to Cover Zones 1 and 2, respectively.

203 *Optimisation approach*

204 A candidate CWDS layout is evaluated by objective functions – mathematical functions which calculate
 205 the performance of the layout with respect to each of the objectives. Here, the candidate CWDS layouts
 206 are evaluated with respect to the percentage of points in each Cover Zone which are visible. The results
 207 correspond to a single point in *objective function space*, as is illustrated in Figure 9 in which a number of
 208 candidate layouts (candidate solutions) have been evaluated. Figure 9 considers a problem instance involving
 209 two Cover Zones, which correspond to the two objectives on the axes. In multi-objective optimisation, the
 210 solutions in Figure 9 are classified as either *non-dominated* or *dominated*.

211 When comparing the non-dominated solutions in Figure 9 to each other, moving from one solution to
 212 another results in an improvement in at least one objective, but the degradation in at least one other
 213 objective. No non-dominated solution is better than another with respect to *all* the objectives. The inferior
 214 solutions that are not included in the non-dominated set are said to be *dominated* by the non-dominated
 215 solutions because at least one non-dominated solution that is better with respect to *all* the objectives exists
 216 for each dominated solution. The non-dominated solutions are sought for decision-making purposes because
 217 they offer superior objective function values and trade-off alternatives to those of the dominated solutions.
 218 The representation of the set of non-dominated solutions is commonly known as the *Pareto-optimal front*,
 219 or simply the *Pareto front*, as they form a frontier in multi-objective space as seen in Figure 9 (Zitzler et al.,

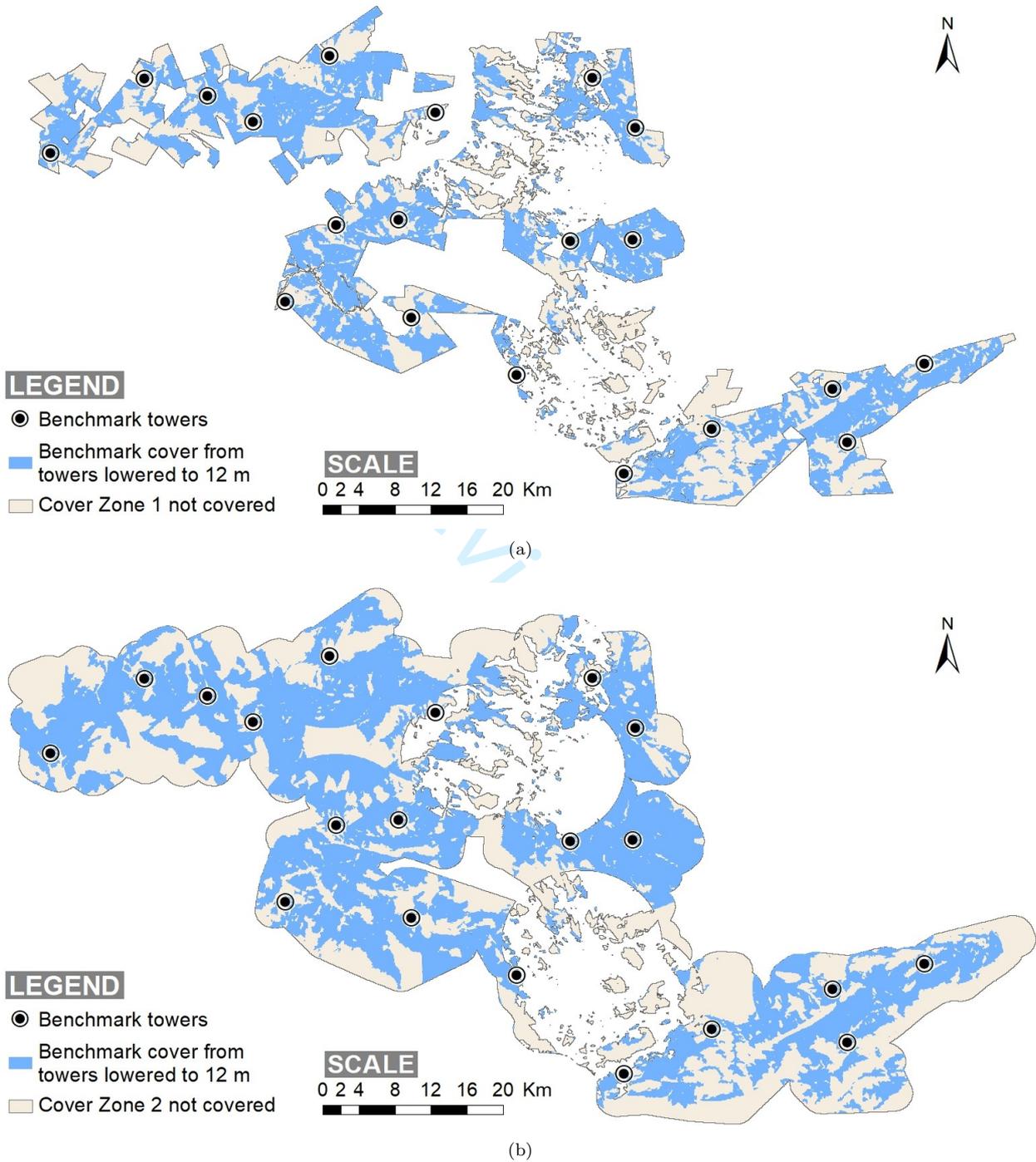


Figure 8: Cover achieved by the twenty benchmark towers, determined with a detection range of 8 km and a simulated height of 12 m, with respect to (a) Cover Zone 1 (56.0%), and (b) Cover Zone 2 (54.6%).

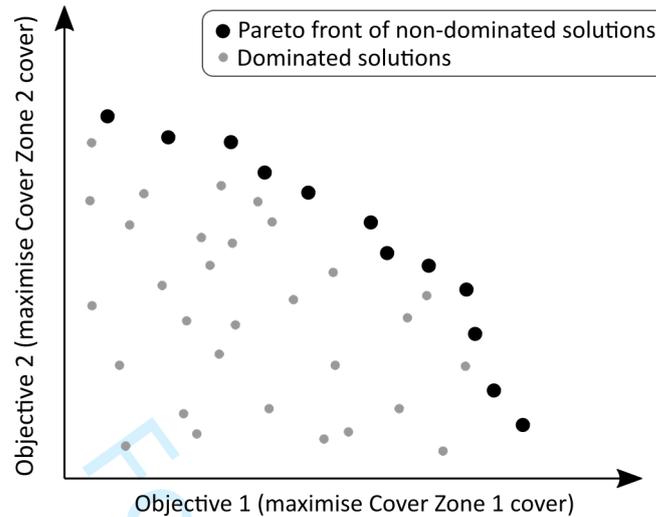


Figure 9: The notions of solution domination and of a Pareto front in objective function space.

220 2004; Knowles et al., 2006). Decision makers need only consider solutions on the Pareto front due to the
 221 superiority of these solutions.

222 One approach to obtaining approximate solutions on the Pareto front is the use of commercial software,
 223 such as CPLEX⁶, and open-source software, such as Gurobi⁷. These software packages take Integer-Linear
 224 Programming formulations of the objective functions and constraints as input. Solving multi-objective
 225 problems with these packages requires transforming the multiple objective functions into a single objective
 226 function using a weighted sum (Cohon, 1978; Murray et al., 2007). The weighted-sum objective function O_s
 227 is given by

$$O_s = \sum_i w_i O_i \quad (1)$$

228 where the objectives O_i are combined using weights w_i . By varying the objective weights in multiple runs,
 229 a Pareto-front approximation may be traced out. However, determining points on the Pareto front in this
 230 manner may require a prohibitively large number of weight combinations when many objectives and large
 231 solution spaces are considered (ReVelle and Eiselt, 2005; Tong et al., 2009). The solution space is the set of
 232 all possible solutions to a problem, *i.e.* all the possible candidate CWDS layouts on the terrain. The number
 233 of possible solutions (N_p) is

$$N_p = \binom{N_s}{N_t} = \frac{N_s!}{N_t!(N_s - N_t)!} \quad (2)$$

234 where N_t and N_s denote the number of towers available for placement and the number of feasible sites,
 235 respectively. Here, 20 tower sites have to be selected from 741 813 sites in the Placement Zone of Figure 5(c)
 236 – a solution space that is sufficiently large to render the use of the weighted-sum approach infeasible.

237 Instead of the weighted-sum approach, powerful metaheuristic optimisation procedures are often em-
 238 ployed in order to approximate the Pareto front within realistic computation times (Zitzler et al., 2004;
 239 Tong et al., 2009). Multi-Objective Evolutionary Algorithms are popular for this purpose and are able to
 240 approximate the Pareto front in a single run (Fonseca and Fleming, 1993; Purshouse and Fleming, 2003).
 241 The Non-dominated Sorting Genetic Algorithm-II (NSGA-II) is a Multi-Objective Evolutionary Algorithm
 242 that has been used extensively in the literature for multi-objective optimisation problems (including applica-
 243 tions that consider covering problems) (Raisanen and Whitaker, 2005; Kim et al., 2008; Kwong et al., 2014;

⁶www.ibm.com/analytics/cplex-optimizer

⁷www.gurobi.com

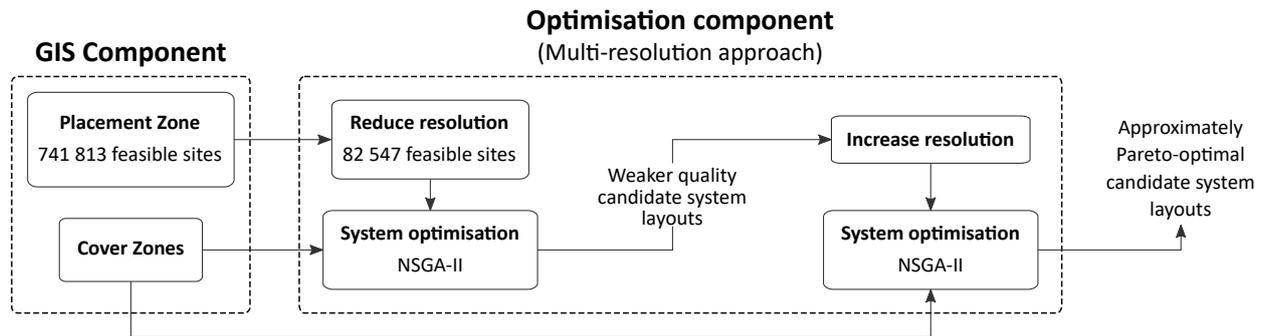


Figure 10: The CWDS tower site-selection optimisation framework followed in this paper.

244 Heyns and van Vuuren, 2016, 2018) and was employed in this paper. More information on Multi-Objective
 245 Evolutionary Algorithms and the NSGA-II may be found in the Appendix.

246 At the highest resolution of terrain data representation (30 m spacing), the number of feasible sites in the
 247 Placement Zone of Figure 5(c) is 741 813. This is significantly more than is generally encountered in facility
 248 location problems (Kim et al., 2004, 2008; Tanergüçlü et al., 2010; Bao et al., 2015), mainly because manual
 249 intervention to reduce the number of possible sites is impractical for the terrain sizes for which this research
 250 is intended. This large number of feasible sites increases the computational complexity of the algorithm by
 251 increasing the number of possible CWDS layouts. In instances such as these, the Multi-Resolution Approach
 252 of Heyns and van Vuuren (2016) may be employed. The Multi-Resolution Approach is an optimisation
 253 tool which was specifically developed for geospatial facility location problems with unusually large solution
 254 spaces. The approach reduces the number of sites considered during the search for the Pareto front by
 255 first solving the problem at a coarse geographic resolution for site selection (exploration), after which a
 256 finer resolution is used around promising site locations and the optimisation process repeated (exploitation).
 257 This results in reduced computational complexity, fewer viewshed computations, and reduced computation
 258 time requirements (Heyns and van Vuuren, 2016). Implementation of the Multi-Resolution Approach results
 259 in little or no reduction in the quality of solution in the Pareto-front approximation, and can even lead to
 260 improved quality in some instances (Heyns, 2016; Heyns and van Vuuren, 2016). Pseudo-code descriptions of
 261 the NSGA-II and its Multi-Resolution Approach implementation are available in the literature (Kim et al.,
 262 2008; Heyns and van Vuuren, 2016).

263 The proposed site-selection optimisation framework is summarised graphically in Figure 10, and is divided
 264 into a GIS component and an optimisation component. The GIS component comprises a) the identification
 265 of suitable candidate sites within the Placement Zone, and b) the determination of the Cover Zones, based
 266 upon smoke layer heights, buffer zones, and existing cover. The Placement Zones and Cover Zones are the
 267 inputs to the optimisation component which performs two runs of the NSGA-II – the difference in each run
 268 being the candidate site inputs as determined by the Multi-Resolution Approach. Here, the first NSGA-II
 269 run takes as input sites which are extracted from the original Placement Zone at a resolution of 90 m between
 270 sites (from the original 30 m resolution), resulting in 82 547 candidate sites. The second NSGA-II run takes
 271 as input the sites included in the candidate layouts returned by the first NSGA-II run, as well as all the
 272 feasible sites at the original, highest 30 m resolution, that are within 60 m of these sites.

273 Due to the stochastic nature of the Pareto-front approximation process of the NSGA-II (see Appendix),
 274 the solutions returned by different optimisation runs generally vary in quality, and it is therefore standard
 275 practice to repeat the process multiple times (Knowles et al., 2006; Kim et al., 2008; Tong et al., 2009).
 276 The results of all the runs are then combined and a final attainment front (the globally best set of the
 277 approximately Pareto-optimal solutions from all optimisation runs) is identified. The process in Figure 10
 278 was repeated forty times, after which additional optimisation was performed as described below.

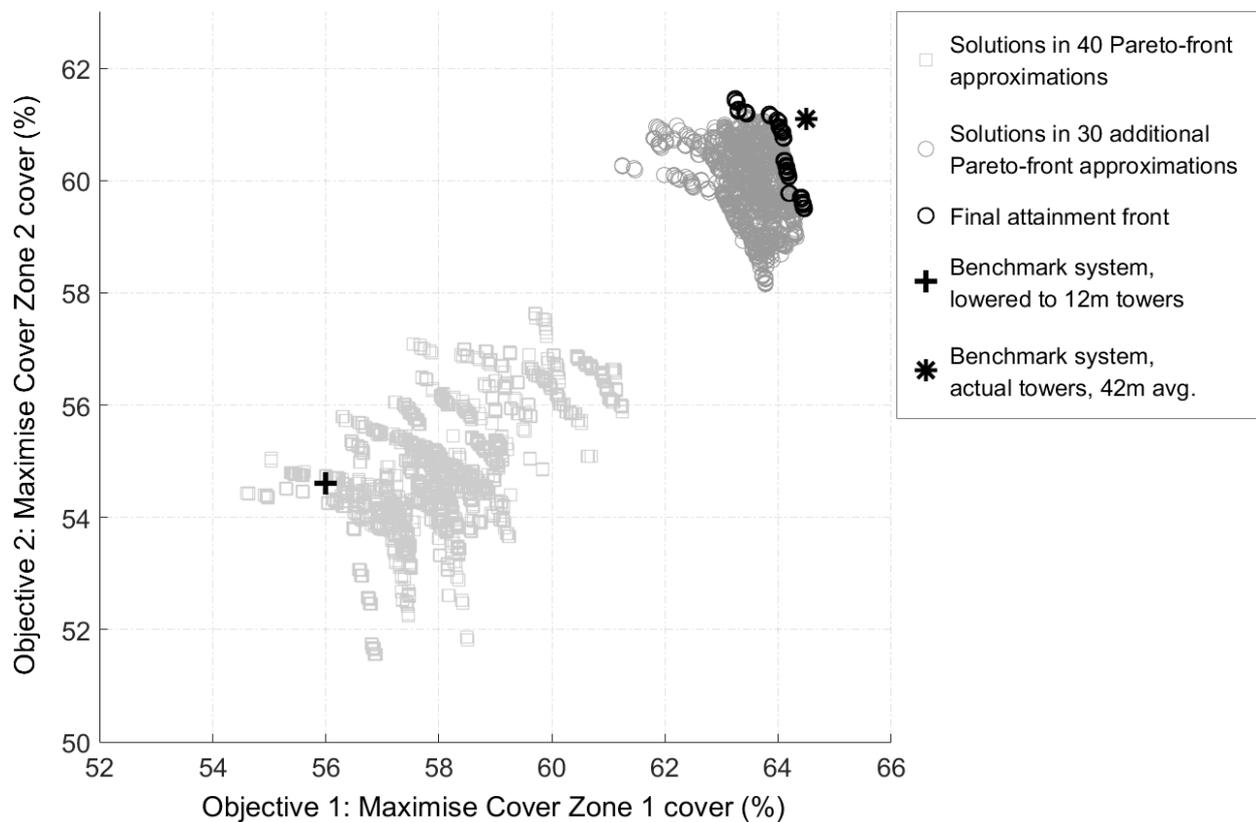


Figure 11: Results in objective function space of multiple runs of the optimisation framework in Figure 10, in which the objective was to place twenty towers at sites within the Placement Zone in Figure 5(c), so that visibility cover with respect to the Cover Zones in Figures 7(c) and (d) is maximised.

279 Results

280 *Pareto-front approximation*

281 The forty Pareto-front approximation generated by the framework in Figure 10 produced a total of
 282 1818 unique solutions, which are shown by the grey squares in objective function space in Figure 11. It is
 283 observed that the benchmark CWDS, evaluated with 12-m towers and indicated by the black cross marker,
 284 is outperformed in at least one objective by most of the optimisation-determined solutions, while being
 285 outperformed in both objectives (*i.e.* dominated) by a large number of these solutions.

286 Upon closer inspection, it was revealed that the solutions returned by the forty optimisation runs are, in
 287 fact, unique combinations of 917 sites (which mostly neighbour other sites), which are shown in Figure 12(a).
 288 Since these sites are included in multiple Pareto-optimal solution approximations, it may be assumed with
 289 confidence that they are higher-quality candidate sites than the other sites in the entire original Placement
 290 Zone of 741 813 sites. It was therefore decided to investigate the use of these 917 sites as a new Placement
 291 Zone for thirty additional optimisation runs – thereby excluding a large number of weaker sites that were
 292 considered in the forty initial optimisation runs, and as a result, limiting the search to better sites only.
 293 These sites were considered as a single level by the NSGA-II and without multi-resolution optimisation.
 294 The 1219 solutions which were contained in the resulting Pareto-front approximations are shown by the
 295 grey circles in Figure 11 – achieving a marked improvement over the solutions returned by the first forty
 296 Pareto-front approximations (the grey squares). The final attainment front contained 72 solutions, which
 297 are indicated by black circle markers in Figure 11. When compared to the benchmark network with 12 m
 298 towers, the solutions contained within the final attainment front exhibit an increase in cover of up to 8.5%

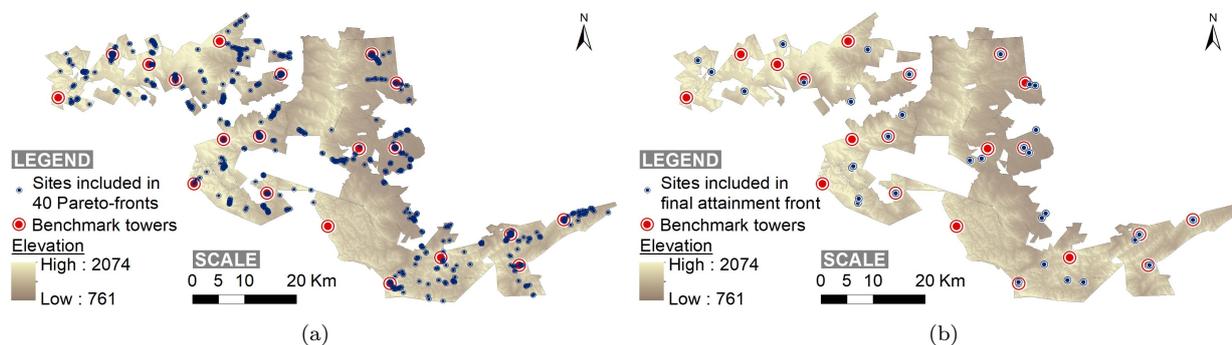


Figure 12: Sites included in (a) the solutions in forty Pareto-front approximations obtained by the framework in Figure 10, and (b) the solutions in the final attainment front in Figure 11 obtained by additional optimisation runs.

299 with respect to Cover Zone 1, while an increase of up to 6.9% is observed with respect to Cover Zone 2.
 300 Most impressive is that these solutions achieve objective-function values that are similar to those achieved
 301 by the benchmark towers when evaluated with their actual heights that average 42 m (the asterisk marker),
 302 and some solutions even outperform these towers with respect to the second objective. The 72 solutions
 303 comprise different combinations of 61 sites which are shown on the client area in Figure 12(b) – a significant
 304 decrease from the 917 sites in Figure 12(a).

305 *Candidate layouts*

306 The site locations and coverage achieved by two solutions on the final attainment front in Figure 11 are
 307 shown with respect to Cover Zone 1 in Figure 13 and Cover Zone 2 in Figure 14. Solution 1 is the solution on
 308 the attainment front that achieves the best coverage with respect to Cover Zone 1, and its site locations are
 309 shown along with its coverage of Cover Zone 1 and Cover Zone 2 in Figures 13(a) and 14(a), respectively.
 310 Solution 2 is the solution on the attainment front that achieves the best coverage with respect to Cover
 311 Zone 2, and Figures 13(b) and 14(b) show its site locations and resulting coverage of the two Cover Zones.

312 A number of similarities may be observed when analysing the proposed sites of these two candidate
 313 layouts. Six sites are, in fact, common to both layouts. When comparing the remainder of the sites, nine
 314 are similarly located in the two layouts and the slight differences in location of between 25 m and 70 m
 315 are indistinguishable in Figures 13 and 14. The remaining five sites in each layout differ more significantly
 316 and are at least 2 km from the nearest site in the other layout. What may be noticed when analysing
 317 these five sites is how their locations in each layout are a result of the objective with respect to which their
 318 layout achieves the best result – an indication of how the multi-objective optimisation process simultaneously
 319 pursues site combinations for different objectives. In Figures 13(a) and 14(a) for Solution 1, these five sites
 320 tend to be located more inward from the boundaries, with the result that their coverage contributes more
 321 to that achieved with respect to the client area in Cover Zone 1, and less with respect to the buffer zone
 322 in Cover Zone 2. In Figures 13(b) and 14(b) for Solution 2, these sites are mostly located closer to the
 323 boundaries, which means that their coverage contributes more to that achieved with respect to the buffer
 324 zone in Cover Zone 2, while reducing cover of the client area in Cover Zone 1.

325 *Expert feedback*

326 A selection of optimised system layouts were presented to a group of experts at the Nelspruit Fire
 327 Protection Agency in the form of Figures 11, 13 and 14. The experts included foresters each with over 20
 328 years of experience in forest and fire management in the region, GIS specialists from forestry clients, and
 329 ForestWatch decision makers and detection centre operators (some of whom were involved in the planning
 330 of the existing CWDS). Physical site locations of candidate layouts were also presented in Google Earth
 331 Pro, allowing proposed sites to be viewed on top of a satellite image representation of the terrain. This

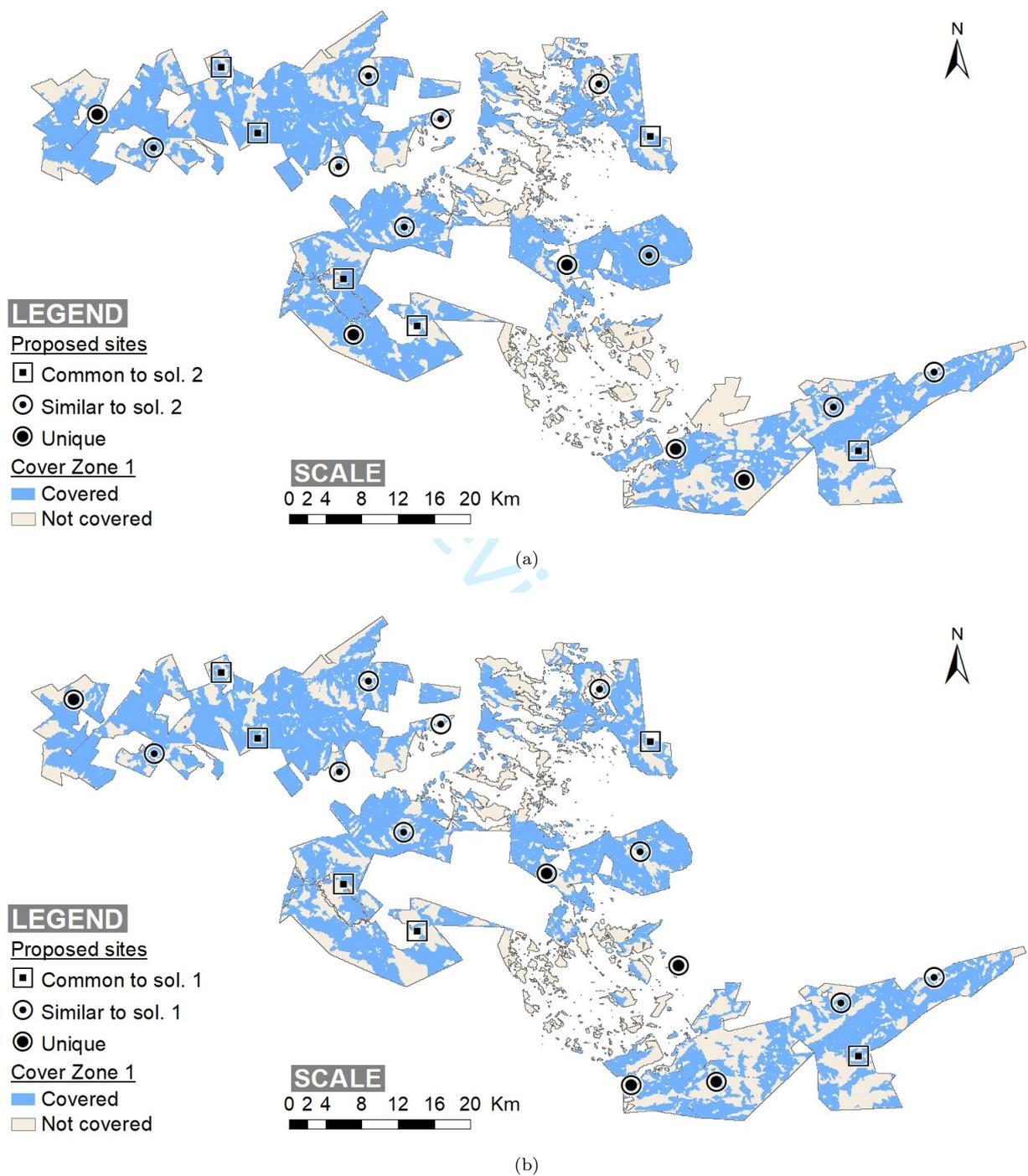


Figure 13: Physical site locations and cover achieved with respect to the Cover Zone 1 for two solutions from the final attainment front in Figure 11. Solution 1 in (a) achieves the best cover with respect to Cover Zone 1, while Solution 2 in (b) achieves the best cover with respect to Cover Zone 2.

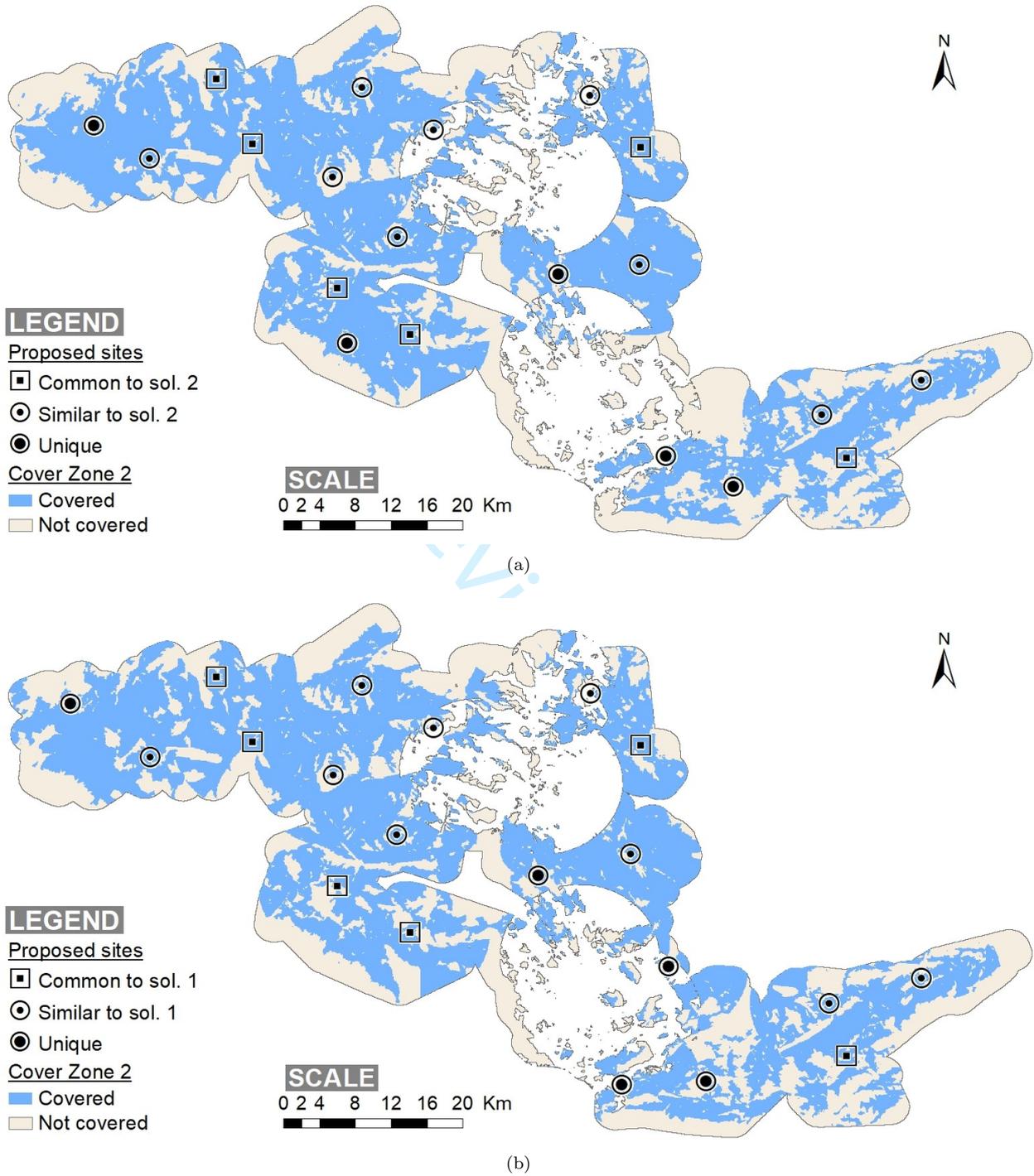


Figure 14: Physical site locations and cover achieved with respect to Cover Zone 2 for the same layouts presented in Figure 13. Solution 1 in (a) achieves the best Cover Zone 1 cover, while solution 2 in (b) achieves the best cover with respect to Cover Zone 2.

332 visualisation provided an effective means of estimating practical site suitability without having to physically
333 visit any of the sites.

334 The experts agreed that the sites comprising the optimised layouts presented were suitable from a prac-
335 tical, real-world perspective, demonstrating the effectiveness of the Placement-Zone determination process
336 outlined above. A few of the sites in each of the candidate system layouts were located precisely at or im-
337 mediately adjacent to actual sites, while others were within 500 m of actual sites. Sites that were considered
338 for tower placement during the original site-selection process, but that were not used, were also present in
339 many of the candidate solutions – this renewed discussions between the experts about these sites' suitability
340 compared to the actual sites. The remaining sites were judged by all those present to be good proposals as
341 well.

342 Discussion

343 The first steps taken towards a comprehensive CWDS tower-site selection optimisation framework have
344 been described. The GIS component of this framework comprises the determination of feasible candidate
345 sites (the Placement Zone) in addition to determining discrete demand points within areas with respect to
346 which visibility cover from the cameras is determined (the Cover Zones). Metaheuristics are applied in the
347 optimisation approach to determine candidate CWDS layouts which aim to achieve optimal results with
348 respect to specific objectives. The Multi-Resolution Approach was used in conjunction with the popular
349 NSGA-II algorithm in the metaheuristic approach, and the objectives were to maximise visibility cover with
350 respect to two different smoke layer levels above the terrain surface. An area in the Nelspruit region in South
351 Africa, which is currently covered by an existing ForestWatch CWDS, was used as the study area, and the
352 optimisation framework was used to compute high-quality trade-off solutions for CWDSs comprising twenty
353 cameras.

354 The framework can provide multiple candidate CWDS layouts in under a week (including data collection,
355 data processing, preliminary analysis and optimisation), compared to the actual site-identification process
356 that spanned over more than five months. The solutions obtained by the optimisation framework were
357 found to significantly outperform the actual configuration with respect to both covering objectives when
358 considering identical tower heights of 12 m. Furthermore, the optimisation-determined solutions achieved
359 similar coverage to the existing system with its actual tower heights – despite the optimisation solutions
360 being limited to 12-m tower heights while the existing system has an average tower height of 42 m. The
361 fact that a 12-m tower costs more than three times less to install than a 42 m tower⁸ is an indication of the
362 potential cost savings that may be achieved by the optimisation approach. The optimised solutions were
363 able to reliably identify the most important sites, thereby further reducing the time required to implement
364 a full CWDS by allowing site visits to focus on sites which are most likely to form part of the final system.

365 The results were presented to experts from ForestWatch and forestry organisations from the Nelspruit
366 region and the feedback was positive. The presented candidate CWDS layouts were considered practically
367 implementable in a real-world scenario, and it was concluded that the optimisation framework is a tool
368 that should be used in future CWDS planning and decision-making processes. Elements of the CWDS
369 site-selection optimisation framework described above have already been used for the planning of new tower
370 sites.

371 In a real-world CWDS site-selection problem, the decision makers would compare results such as those
372 presented in Figures 11, 13 and 14 in terms of objective-function values and tower site locations in order
373 to make a final decision. A set of solutions that is diverse with respect to objective-function values and
374 tower site locations is desirable in order to provide a good set of alternatives that may be considered, and
375 this goal has been achieved as shown in Figures 11 and 12(a). It is possible, however, that attainment
376 fronts consisting of an undesirably large number of solutions may be returned, *e.g.* the 72 solutions in
377 the attainment front in Figure 11. Many of these solutions offer negligible trade-offs in terms objective-
378 function values and tower-site locations, rendering decision making a long and tiresome process (Heyns,

⁸These costs were determined from tower installation costs provided by ForestWatch technicians.

379 2016). In future work, techniques to filter the Pareto-front to generate a smaller number of solutions should
380 be investigated. Possible techniques include those that are performed in objective-function space, such as
381 the epsilon-grid method (Mavrotas, 2009), and those performed in physical solution space, such as site
382 proximity-dependent de-clustering investigated by Heyns (2016).

383 Two smoke layers and a buffer zone were used for the Cover Zones with respect to which a CWDS's smoke
384 detection potential was evaluated. In future work, additional Cover Zones may include certain priority areas
385 within the larger area to be covered. Examples may include areas around key infrastructure points such
386 as power plants and chemical storage facilities. In such instances, a priority Cover Zone is simply added
387 as an additional covering objective and the problem solved as usual by the multi-objective optimisation
388 framework. If desired, decision makers may then turn their focus toward solutions that perform well with
389 respect to the priority areas in determining a suitable layout.

390 Conflict of interest

391 The authors declare no conflicts of interest.

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403 Appendix – Multi-objective evolutionary algorithms

404 A popular alternative to the weighted-sum approach is Multi-Objective Evolutionary Algorithms, which
405 are able to approximate a diverse set of trade-off solutions on the Pareto front in a single run (Fonseca and
406 Fleming, 1993; Purshouse and Fleming, 2003) and are also known to achieve good results fast (Alp et al.,
407 2003). Multi-Objective Evolutionary Algorithms iteratively evolve a population of candidate solutions to an
408 optimisation problem based on natural principles (Cheshmehgaz et al., 2015). An initial, randomly generated
409 population of candidate solutions undergoes carefully controlled evolution over multiple generations, finally
410 arriving at a set of solutions that approximate the Pareto front (Deb et al., 2002; Cheshmehgaz et al., 2015).
411 It has been shown how a Multi-Objective Evolution Algorithm may find more non-dominated solutions than
412 are found by a weighted-sum approach, and as a result, may achieve a superior Pareto-front approximation
413 to a weighted-sum approach (Kim et al., 2008). Examples of the application of Multi-Objective Evolutionary
414 Algorithms to placement problems include the placement of transmitters (Meunier et al., 2000; Raisanen and
415 Whitaker, 2005), wind turbines (Kwong et al., 2014; Yamani Douzi Sorkhabi et al., 2016), and observation
416 equipment (Kim et al., 2004; Tong et al., 2009; Bao et al., 2015; Heyns and Van Vuuren, 2015; Heyns and
417 van Vuuren, 2018).

418 The NSGA-II is a Multi-Objective Evolutionary Algorithm that is classified as a *genetic algorithm*, in
419 which a candidate CWDS layout is represented as a *chromosome* string of N_t feasible tower site numbers
420 (Deb et al., 2002; Heyns and van Vuuren, 2016). Site numbers are pre-determined by an indexing scheme
421 for all the sites within the Placement Zone's raster representation and are typically derived with respect to
422 row and column indices (Heyns and van Vuuren, 2016). For example, a chromosome [33, 125, 8 333, 12 045]
423 represents a candidate CWDS with four towers located at sites 33, 125, 8 333 and 12 045.

424 The NSGA-II iteratively performs evolution-inspired selection processes and modification operators on a
425 randomly generated population of such candidate CWDS chromosomes until a termination criterion is met
426 (Deb et al., 2002). A typical termination criterion is when the algorithm has reached a point where successive
427 populations fail to significantly improve on the solution quality of previous generations (Heyns, 2016). Two
428 mechanisms are utilised in order to adequately explore the solution space. Crossovers performed between
429 sub-strings of parent chromosomes create new offspring solutions that consist of new site combinations,
430 without altering the constituent sites that are inherited from the parent solutions (Deb et al., 2002; Heyns
431 and van Vuuren, 2016). Parents are randomly selected for crossover, although solutions which perform
432 well with respect to the objective functions are favoured – meaning that the offspring solutions typically
433 exhibit some of the strong properties of their parents. After crossover, mutation promotes site diversity
434 by stochastically introducing new, unexplored site locations into the chromosomes, as opposed to merely
435 exchanging already explored sites by means of crossover (Deb et al., 2002; Heyns and van Vuuren, 2016).

For Review Only

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