## First double-differential measurement of kinematic imbalance in neutrino interactions with the MicroBooNE detector

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We report the first measurement of flux-integrated double-differential quasielastic-like neutrinoargon cross sections, which have been made using the Booster Neutrino Beam and the MicroBooNE detector at Fermi National Accelerator Laboratory. The data are presented as a function of kinematic imbalance variables which are sensitive to nuclear ground state distributions and hadronic reinteraction processes. We find that the measured cross sections in different phase-space regions are sensitive to different nuclear effects. Therefore, they enable the impact of specific nuclear effects on the neutrino-nucleus interaction to be isolated more completely than was possible using previous single-differential cross section measurements. Our results provide precision data to help test and improve neutrino-nucleus interaction models. They further support ongoing neutrinooscillation studies by establishing phase-space regions where precise reaction modeling has already been achieved.

Neutrino oscillation measurements aim to extract neutrino mixing angles, mass differences, and the chargeparity violating phase, and to search for new physics beyond the Standard Model [1-3]. The analysis of such measurements traditionally relies on detailed comparisons of measured and theoretically-expected neutrino interaction rates in the corresponding detectors. Therefore, a precise understanding of neutrino-nucleus interactions is required to fully exploit the discovery potential of current and next-generation experiments.

With a growing number of neutrino-oscillation experiments employing liquid argon time projection chamber (LArTPC) neutrino detectors [4–9], high-accuracy modeling of neutrino-argon interactions is becoming of paramount importance [10–12]. The overarching goal of these efforts is both to achieve few-percent-level modeling of neutrino-argon interaction rates and to provide a detailed understanding of the final-state kinematics of emitted particles that are used to reconstruct the energies of the interacting neutrinos [13, 14].

This Letter reports the first measurement of fluxintegrated double-differential cross sections for muonneutrino-argon ( $\nu_{\mu}$ -Ar) charged-current (CC) quasielastic (QE)-like scattering reactions as a function of transverse kinematic imbalance variables. Building upon a previous analysis of neutrino-argon cross sections with a similar signal event topology [15], we focus on reactions where the neutrino removes a single intact proton from the nucleus without producing any additional detected particles. The results reported here are obtained using the Booster Neutrino Beam (BNB) and the MicroBooNE detector at Fermi National Accelerator Laboratory with an exposure of  $6.79 \times 10^{20}$  protons on target. Transverse kinematic imbalance variables were previously shown to be sensitive to the modeling of the nuclear ground-state distribution and to nuclear medium effects, such as hadronic final-state interactions (FSI) [16–21]. By measuring the components of the muon and proton momenta perpendicular to the neutrino direction,  $\vec{p}_T^{\ \mu}$ and  $\vec{p}_T^{\ p}$  respectively, we construct the transverse missing momentum,  $\delta \vec{p}_T = \vec{p}_T^{\ \mu} + \vec{p}_T^{\ p}$ , and its angular orienta-

tion with respect to  $\vec{p}_T^{\ \mu}$ ,  $\delta \alpha_T = \arccos \left( -\frac{1}{2} \right)$ 

$$\frac{-p_T \mu \delta p_T}{p_T \mu \delta p_T} \bigg)$$

Due to the isotropic nature of Fermi motion,  $\delta \alpha_T$  is expected to be uniformly distributed in the absence of any FSI. In the presence of FSI, the proton momentum is generally reduced and the  $\delta \alpha_T$  distribution becomes enhanced towards 180°. Similarly, the shape of the  $\delta p_T$  distribution encapsulates information related to Fermi motion and is further smeared due to FSI and multi-nucleon effects. Given the sensitivity of  $\delta \alpha_T$  to FSI and of  $\delta p_T$ to both FSI and Fermi motion, a simultaneous measurement of these two observables can help to disentangle the individual impact of each nuclear effect on the neutrinonucleus interaction. Similarly, the muon-proton momentum imbalance components transverse and parallel to the transverse lepton momentum,  $\delta p_{T,x} = \delta p_T \cdot \sin \delta \alpha_T$  and  $\delta p_{T,y} = \delta p_T \cdot \cos \delta \alpha_T$ , provide further handles on Fermi motion and FSI processes, respectively.

The active volume of the MicroBooNE LArTPC contains 85 tonnes of argon [22]. It is exposed to the BNB neutrino energy spectrum that peaks around 0.8 GeV and extends to about 2 GeV.

Neutrinos are detected by measuring the charged particles produced following their interactions with argon



FIG. 1. The flux-integrated (a) single- and (b-c) double- (in  $\delta \alpha_T$  bins) differential CC1p0 $\pi$  cross sections as a function of the transverse missing momentum  $\delta p_T$ . Inner and outer error bars show the statistical and total (statistical and shape systematic) uncertainty at the 1 $\sigma$ , or 68%, confidence level. The gray band shows the separate normalization systematic uncertainty. Colored lines show the results of theoretical cross section calculations with (solid line) and without (dashed line) FSI based on the GENIE (blue) and GiBUU (orange) event generators.

nuclei in the LArTPC active volume. These charged particles travel through the liquid argon, producing both scintillation light and trails of ionization electrons. In the presence of a uniform 273 V/cm electric field, the ionization electrons drift through the argon and are detected by a system of three anode wire planes that are perpendicular to the field. The scintillation light is measured by photomultiplier tubes (PMTs). Events are recorded if the PMT signals are in time coincidence with the beam arrival time. Trigger hardware and software selection cuts reject background events, mostly from cosmic muons, providing enriched data samples in which a neutrino interaction occurs in  $\approx 15\%$  of selected beam spills [23].

The Pandora reconstruction package [24] is used to form individual tracks from the measured ionization signals in the enriched data samples. Particle identification and momentum determination are performed using the measured track energy-deposition profile and track length [25, 26].

Candidate muon-proton pairs are identified by requiring exactly two track-like objects and no shower-like objects based on a track-score variable from Pandora [27, 28]. The discriminant described in [29] is used to distinguish muon and proton candidates. We further apply quality cuts to avoid mis-reconstructed tracks. Details are given in [30].

To reduce contributions from cosmic tracks and to minimize bin-migration effects, the event selection considers only muon and proton track pairs that are fully contained within a fiducial volume of 10 cm from the edge of the detector active volume.

The signal definition used in this analysis includes all  $\nu_{\mu}$ -Ar scattering events with a final-state muon with momentum  $0.1 < p_{\mu} < 1.2 \,\text{GeV}/c$  and exactly one final-state proton with  $0.3 < p_p < 1 \,\text{GeV}/c$ . Events with final-state neutral pions at any momentum are excluded. Signal events may contain additional protons with momentum less than 300 MeV/c or greater than  $1 \,\text{GeV}/c$ , neutrons at any momentum, and charged pions with momentum lower than 70 MeV/c. We refer to the signal events as  $CC1p0\pi$ . Due to the requirement for a single proton and no pions in the final state, the  $CC1p0\pi$  topology of interest is dominated by QE events. Yet, more complex interactions, namely meson exchange currents (MEC), resonance interactions (RES) and deep inelastic scattering events (DIS), can still produce the  $CC1p0\pi$  experimental signature. Events that do not satisfy the  $CC1p0\pi$  signal definition at a truth level are treated as background. Such events are referred to as non- $CC1p0\pi$  and are dominated by interactions with two protons in the momentum range of interest, where the second proton was not reconstructed. This topology is studied in [31], where a good data-simulation agreement is observed.

After the application of the event selection, we retain 9051 data events that satisfy all criteria. Event distributions for all the aforementioned variables of interest and details on the CC1p0 $\pi$  event selection , along with the corresponding systematic uncertainties, can be found in the Supplemental Material and in [30].

The flux-averaged differential event rate as a function of a given variable x in bin i is obtained by

$$\frac{dR}{dx_i} = \frac{N_i - B_i}{T \cdot \Phi_\nu \cdot \Delta_i} \tag{1}$$

where  $N_i$  and  $B_i$  are the number of measured events and the expected background events, respectively. T is the number of target argon nuclei in the fiducial volume of interest.  $\Phi_{\nu}$  corresponds to the total BNB flux and, finally,  $\Delta_i$  corresponds to the *i*-th bin width or area for the single- and double-differential results, respectively.

We report the extracted cross sections for the measured interaction using the Wiener singular value decomposition (Wiener-SVD) unfolding technique as a function of unfolded kinematic variables [32]. More details on the unfolding procedure can be found in [30]. The unfolding machinery returns the unfolded differential cross section and the corresponding uncertainties. Apart from the unfolded result, an additional smearing matrix  $A_C$ 



FIG. 2. The flux-integrated (a) single- and (b-c) double- (in  $\delta p_T$  bins) differential CC1p0 $\pi$  cross sections as a function of the angle  $\delta \alpha_T$ . Inner and outer error bars show the statistical and total (statistical and shape systematic) uncertainty at the 1 $\sigma$ , or 68%, confidence level. The gray band shows the separate normalization systematic uncertainty. Colored lines show the results of theoretical cross section calculations with a number of FSI-modeling choices based on the GENIE event generator.

is obtained, which accounts for the regularization and bias of the measurement. When a comparison to the unfolded data is performed, the corresponding  $A_C$  matrices must be applied to the true cross section predictions. See Supplemental Material for the data release, the unfolded covariance matrices, and the additional matrices  $A_C$ .

As in previous MicroBooNE measurements [15, 33–35], the full Monte Carlo (MC) simulation used in the unfolding procedure consists of a combination of simulated neutrino interactions overlaid on beam-off background events. This provides an accurate description of the dominant cosmic backgrounds pertinent to surface detectors using real data. Neutrino interactions are simulated using the GENIE v3.0.6 event generator [36, 37]. The CC QE and CC meson exchange current (MEC) neutrino interaction models have been tuned to T2K  $\nu_{\mu}$ -<sup>12</sup>C CC0 $\pi$ data [38, 39]. Predictions for more complex interactions, such as resonances, remain unaltered. No additional MC constraints are applied. We refer to the corresponding prediction as G18. The latter configuration is used to simulate both CC1p0 $\pi$  signal and non-CC1p0 $\pi$  background events. GENIE generates all final-state particles associated with the primary neutrino interaction and propagates them through the nucleus, accounting for FSI. The particle propagation outside the nucleus is simulated using GEANT4 [40], with the MicroBooNE detector response modeled using the LArSoft framework [41, 42]. Based on this simulation, we estimate that our efficiency for selecting fully contained CC1p0 $\pi$  events is  $\approx 10\%$ , with a purity of  $\approx 70\%$ .

The total covariance matrix  $E = E^{\text{stat}} + E^{\text{syst}}$  used in the Wiener-SVD filter includes the statistical and systematic uncertainties associated with our measurement.  $E^{\text{stat}}$  is a diagonal covariance matrix including the statistical uncertainties and  $E^{\text{syst}}$  is a covariance matrix incorporating the total systematic uncertainties. More details on the sources of systematic uncertainty and the construction of these matrices can be found in [30]. These matrices include uncertainties on the integrated cross section due to the neutrino flux prediction (7.3%) [43], neutrino interaction cross section modeling (6%) [36, 37, 39], detector response modeling (4.9%) [44], beam exposure (2.3%), statistics (1.5%), number-of-scattering-targets (1.15%), reinteractions (1%) [45], and out-of-cryostat interaction modeling (0.2%). The full fractional uncertainty on the integrated total cross section sums to 11%.

Across the results reported in this Letter, statistical uncertainties are shown by the inner error bars on the final results. The systematic uncertainties were decomposed into shape- and normalization-related sources following the procedure outlined in [46]. The cross-term uncertainties were incorporated in the normalization part. The outer error bars on the reported cross sections correspond to statistical and shape uncertainties added in quadrature. The normalization uncertainties are presented with the gray band at the bottom of our results.

The single- and double-differential results as a function of  $\delta p_T$  are presented in Fig. 1. They are compared with G18 and the theory-driven GiBUU 2021 (GiB) event generator. Additional comparisons to the corresponding event generators when FSI are turned off are also included (G18 no-FSI and GiBUU no-FSI). G18 uses the local Fermi gas (LFG) model of the nuclear ground state [47] and the Nieves CCQE scattering prescription [48] with Coulomb corrections for the outgoing muon [49] and random phase approximation (RPA) corrections [50]. It also uses the Nieves MEC model [51], the KLN-BS resonance (RES) [52–55] and Berger-Sehgal coherent (COH) [56] scattering models. Furthermore, the hA2018 FSI model [57] and the MicroBooNE-specific tuning of model parameters [39] are utilized. GiBUU uses somewhat similar models, but, unlike GENIE, they are implemented in a coherent way by solving the Boltzmann-Uehling-Uhlenbeck transport equation [58]. The simulation includes the LFG model [47], a standard CCQE expression [59], an empirical MEC model and a dedicated spin-dependent resonances amplitude calculation following the MAID analysis [58]. The deep inelastic (DIS)



FIG. 3. The flux-integrated (a) single- and (b-c) double- (in  $\delta p_{T,y}$  bins) differential CC1p0 $\pi$  cross sections as a function of the transverse three-momentum transfer component,  $\delta p_{T,x}$ . Inner and outer error bars show the statistical and total (statistical and shape systematic) uncertainty at the 1 $\sigma$ , or 68%, confidence level. The gray band shows the separate normalization systematic uncertainty. Colored lines show the results of theoretical cross section calculations with a number of event generators. The standard deviation ( $\sigma_{\text{Data}}$ ) of a Gaussian fit to the data is shown on each panel.

model is from PYTHIA [60]. The FSI treatment is different as the hadrons propagate through the residual nucleus in a nuclear potential which is consistent with the initial state.

The single-differential results as a function of  $\delta p_T$  using all the events that satisfy our selection are shown in Fig. 1a. The  $\chi^2$ /bins data comparison for each generator shown on all the results takes into account the total covariance matrix, including the off-diagonal elements. Theoretical uncertainties on the models themselves are not included. The peak height of both generator predictions is  $\approx 30\%$  higher when FSI effects are turned off. Yet, all distributions illustrate a transverse missing momentum tail that extends beyond the Fermi momentum ( $\approx 250 \,\mathrm{MeV}/c$ ) whether FSI effects are incorporated or not. The double-differential result using events with  $\delta \alpha_T < 45^\circ$  shown in Fig. 1b is dominated by events that primarily occupy the region up to the Fermi momentum and do not exhibit a high-momentum tail. The doubledifferential results using events with  $135^{\circ} < \delta \alpha_T < 180^{\circ}$ are shown in Fig. 1c and illustrate high transverse missing momentum up to  $1 \,\mathrm{GeV}/c$ . The prediction without FSI effects is strongly disfavored. The region around  $0.3 \,\mathrm{GeV/c}$  in Fig. 1c shows a noticeable difference between the G18 and GiBUU predictions. This behavior could be driven by the different approaches of simulating the MEC and FSI effects between the two event generators, as can be seen in the interaction breakdown of the relevant cross sections in the Supplemental Material. Therefore, the high  $\delta p_T$  region is an appealing candidate for neutrino experiments to benchmark and tune the FSI modeling in event generators. The same single- and double-differential cross section comparisons as a function of  $\delta p_T$  using different FSI variations are included in the Supplemental Material.

Extracted cross sections as a function of  $\delta \alpha_T$  are shown in Fig. 2. Here we perform comparisons to the recently added theory driven GENIE v3.0.6 G21\_11b\_00\_000 configuration (G21 hN) [61]. This configuration uses the SuSAv2 model for CCQE and CCMEC interactions [62], and the hN2018 FSI model [63]. The modeling choices for RES, DIS, and COH interactions are the same as for G18. We investigated the effect of the FSI-modeling choice by comparing the G21 hN results to the ones obtained with G21 hA, where the hA2018 FSI model was used instead, and to G21 G4 with the recently coupled GEANT4 FSI framework [64]. The prediction where the FSI effects have been turned off (G21 no-FSI) is also included for comparison. The impact of different QE modeling options as a function of the same variables is investigated in the Supplemental Material.

The single-differential results as a function of  $\delta \alpha_T$  using all the events that satisfy our selection are shown in Fig. 2a. The prediction without FSI shows a uniform behavior as a function of  $\delta \alpha_T$  and is disfavored by the data. The addition of FSI effects leads to a  $\approx 30\%$  asymmetry around  $\delta \alpha_T = 90^\circ$ . The three FSI models used here for comparison yield a consistent behavior. The double-differential result shown in Fig. 2b using events with  $\delta p_T < 0.2 \,\mathrm{GeV}/c$  illustrates a uniform distribution indicative of the suppressed FSI impact in that part of the phase-space. The G21 no-FSI prediction is higher than the other FSI predictions. The difference comes from the generation of multiple particles above detection threshold due to reinteraction effects in the FSI-rich samples. Such events do not satisfy the signal definition and therefore introduce the difference in the absolute scale. The double-differential results using events with  $\delta p_T >$  $0.4 \,\mathrm{GeV}/c$  are shown in Fig. 2c and illustrate the presence of strong FSI effects with a significantly enhanced asymmetry around 90°. Thus, the high  $\delta \alpha_T$  region is highly informative for the FSI-modeling performance in event generators. See Supplemental Material for details on the interaction breakdown of the aforementioned results and [30] for further double-differential results.

Finally, Fig. 3 shows the single- and double-differential results as a function of  $\delta p_{T,x}$ . The result shows the comparison between the nominal G18 model using the lo-

cal Fermi gas (LFG) and predictions using the same G18 interaction modeling but different nuclear ground-state model options available in the GENIE event generator, namely the Bodek-Ritchie Fermi Gas (RFG) [65] and an effective spectral function (EffSF) [66]. Furthermore, the prediction without RPA effects is shown for comparison (no-RPA) [50]. The FSI impact on the same results in investigated in the Supplemental Material.

The single-differential result (Fig. 3a) illustrates a fairly broad symmetric distribution centered around  $0 \,\mathrm{GeV}/c$ . The double-differential result for events where  $\delta p_{T,y} < -0.15 \,\mathrm{GeV}/c$  (Fig. 3b) illustrates an even broader distribution, as can be seen in the widths ( $\sigma_{\text{Data}}$ ) of Gaussian fits on the data distributions. Conversely, the double-differential result for events with  $|\delta p_{T,y}| <$  $0.15 \,\mathrm{GeV}/c$  (Fig. 3c) shows a much narrower peak which strongly depends on the choice of the underlying model and the inclusion or absence of nuclear effects such as RPA. The LFG and no-RPA predictions are favored in both parts of the phase-space. Both the RFG and EffSF predictions illustrate a poor performance in the double-differential measurements and particularly in the QE-dominated  $|\delta p_{T,y}| < 0.15 \,\text{GeV}/c$  region. The FSImodeling impact on the same  $\delta p_{T,x}$  cross sections is presented in the Supplemental Material. The latter further contains details on the interaction breakdown of various generator predictions for the results reported here, and further single- and double-differential results can be found in [30].

In summary, we report the first measurement of muon neutrino double-differential cross sections on argon as a function of kinematic imbalance variables for event topologies with a single muon and a single proton detected in the final state. We identify parts of the phase space where the Fermi motion can be largely disentangled from FSI and multi-nucleon effects. This disentanglement provides leverage to improve separate parts of the complicated neutrino interaction models that affect single-differential distributions in similar ways. Therefore, the reported results pave the path to substantially reducing cross section systematic uncertainties which will enable precision measurements of fundamental neutrino properties.

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